**CS156 – Introduction to Artificial Intelligence Final Exam Review**

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**Introduction to Agents**

An agent perceives its **environment** through **sensors** and acts upon the environment through **actuators**.

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| **Turing Test** – A test where a human poses a series of questions to the computer and after seeing the responses cannot distinguish the **responses** from those of a human.  **Components Needs to Pass the Turing Test:**  1. **Natural Language Processing**  2. **Knowledge Representation** (i.e. storage paradigm)  3. **Automated Reasoning**  4. **Machine Learning** | **Total Turing Test** – A variant of the Turing Test where the robot passes entirely as a human.  **Additional Requirements Over Standard Turing Test:**  1. **Computer Vision**  2. **Robotics** | **Rational Agent** – For **every possible percept sequence**, the rational agent selects the action it expects to **maximize its** **performance measure** given the information in the **percept sequence** and whatever **built-in knowledge** it has.  **The maximizing action depends on:**  1. **Performance Measure**  2. **Any prior/built-in knowledge of the agent**  3. **Percept sequence to date.**  4. **Set of possible actions.** | **Percept** – An agent’s perceptual inputs through **sensors** at any given instant.  **Percept Sequence** – Set of all percepts to date. |

**Agent Function:** **Map from percept sequences to an agent action**. **Example:** An agent action table.

Agents run an agent program. The agent program runs on the **agent architecture**. The combination of the **agent program** and agent architecture is called a **complete agent**.

**Cognitive Science:** Brings together computer models from AI and experimental techniques from psychology to construct precise and testable theories of the human mind.

**Task Environment (PEAS)**

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| **Performance Measure (P)** – Targets/goals the agent will try to achieve. | **Environment (E)** – Objects that interact with the agent or the agent interacts with | **Actuators (A)** – Tool(s) used by the agent to interact with the environment. | **Sensors (S)** – Tool(s) used by the agent to perceive the environment. |

**Properties of a Task Environment**

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| **Fully Observable vs. Partially Observable**  Can the agent see the entire environment **at once** (e.g. chess)? If not, it may keep a history of what it has observed (taxi-driver). | **Deterministic vs. Stochastic**  Is the next state completely determined by the current state and the action (chess)? Otherwise it is stochastic (taxi-driver). | **Single-Agent vs. Multi-agent**  Do objects in the environment need to be treated as other agents? Multi-agent environments can be **competitive** (chess) or **cooperative** (taxi-driving). **Communication** between agents is possible as is **randomized behavior** to avoid predictability. | **Episodic vs. Sequential**  In an episodic environment, the agent’s experience is divided into episodes. In an episode the agent receives **one percept** and performs **one action** (e.g. quality control robot). In sequential environments, **current actions affect future actions**. |
| **Static vs. Dynamic**  Does the environment **change while the agent is making a decision**? Chess is static while taxi driving is dynamic. | **Discrete vs. Continuous**  Time, percepts, and actions divided **into a fixed, finite set** (e.g. chess)? A continuous environment is taxi-driving. | **Known versus Unknown**  In a known environment, all outcomes of actions are known. In an unknown environment, the agent needs to figure out how it works to make good decisions. |  |

**Example Episodic Agent**

Quality Assurance robot.

* **Performance Measure:** Fixed minimum and maximum tolerances for a widget. (Example ball board min/max weight, diameter, roundess)
* **Environment:** Widget (example ball bearing) received for inspection on an input system. Good bin and discard bins.
* **Actuator:** Arm to place widget in either discard bin or good bin.
* **Sensor:** Check ball bearing weight, diameter, roundness etc.

**Types of Agent Programs**

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| **Simple Reflex Agent** – Select actions based off the **current percept only.** Often defined by **condition-action rules** (i.e. **productions**) | **Model-Based Reflex Agent** – Similar to a Finite State Automata. Uses **internal states** to keep track of the environment. Updates the internal state based off how the environment evolves independently and how the agent’s action affect the environment. This is called the agent **model**. |
| **Goal Based Agents** – A **goal** is a binary condition (i.e. either met or not met). A goal based agent tries to reach a target goal. **Search and planning agents** may be goal based agents. | **Utility Based Agent** – Agent applies a **utility function** to its performance. Agent tries to maximize its overall utility function. |

**Additional Definitions**

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| **Problem solving agents** deal with **atomic environments** (i.e. the environment is treated as a single whole and is **indivisible**). | **Planning agents** deal with **factored or structured environments** (i.e. the environment has **attributes**/**variables** each of which has a **value**). | **Search** – Process of looking over a sequence of actions. | **Solution** – A sequence of actions that takes the agent from the initial state to the goal state. |

**Search Problems**

**Classical search problems** are **deterministic**, **fully-observable**, **known**, and the solution is a **sequence of actions**.

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| **Solution:** A sequence of actions that takes the agent from the initial state to the goal state. | **Root**: Initial State  **Edge/Branches**: Actions  **Node/Vertices**: States in the state space  **Leaf**: A node with no children | **Node Expansion** – Applying all legal actions to the node and **generating** all successor states. | **Frontier or Open List** – Set of successor nodes that have not yet been expanded. |
| **Search Strategy:** Method for choosing the node on the frontier to next expand. | **Repeated State:** Any state visited more than once during a search.  **Redundant Path:** Any two or more paths that go to the same state. | **Closed or Explored Set:** States that have already been expanded. | **Loopy Path** – Where a repeated state is expanded causing you not to continue to explore the same section of a graph. |

**Definitions:**

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| **Uniformed Search** – Also known as (**Blind Search**) is any search that has no information on the search space. | **Informed Search** – Uses **heuristics** that inspect the state space to prioritize moves. | **Explored Set** – Set of all nodes already visited. |
| **Branching Factor (*b*)** – Number of branches/children/successors from a given node. Generally lists as the **maximum branching factor.** | **Depth (*d*)** – Number of branches/children/successors from a given node. | **Frontier Set** – Set of all nodes available for expansion. |

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| **A Problem consists of five attributes:**  1. **Initial State**  2. **Set of possible actions** (ACTIONS)  3. **Successor Function/Transitional Model** (RESULTS)  4. **Goal test** (TERMINAL-TEST)  5. **Cost Function** | **Four Ways to Rate/Measure a Search Strategy:**  1. **Completeness** – If a solution exists, does the algorithm always find it?  2. **Optimal** – Is the solution found by the algorithm always optimal (i.e. have the lowest cost).  3. **Time Complexity** – Amount of time required by the algorithm to perform the search.  4. **Space Complexity** – Amount of memory required by the algorithm to perform the search. |

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| **Name** | **Memory Complexity** | **Time Complexity** | **Complete** | **Optimal** | **Queue Type Used** | **Comments** |
| Depth Limited Search |  |  | No | No | Stack | is the maximum allowed depth.  1. Incomplete if  2. Can be non-optimal if |
| Depth-First Search |  |  | Yes if the graph is finite, No otherwise | No | Stack | 1. Not complete because of the infinite branching problem (e.g. loop).  2. Can be considered special case of depth-limited search with  **Always expand left most node that can be expanded.** |
| Iterative Deepening Depth First Search |  |  | Yes | Yes | Stack | Calls Depth Limited Search algorithm times |
| Breadth First Search |  |  | Yes | Yes if uniform step cost | Queue | Can be considered a variant of uniform cost search where each step cost is the same.  **Expand the root node and then expand all children of the root node in the order they are encountered until all nodes are expanded or a goal is reached.** |
| Bidirectional Search |  |  | Yes | Yes if uniform step cost | Queue | Variant of Breadth-First Search where two breadth first searches (one from start and one from the goal) are initiated and carried out simultaneously.  **Generalization of Breadth-First where the root (i.e. initiate state) node is expanded first and nodes are expanded based of their non-decreasing distance/cost from the root.** |
| Uniform Cost Search |  |  | Yes | Yes | Priority Queue | Variant of Breadth-First Search where the step cost is not uniform.  - Minimum (optimal) cost to the goal.  - Minimum step cost |
| Greedy Best First Search | N/A | N/A | No | No | None | Selects node for expansion based off the one with the **lowest heuristic cost**.  Can oscillate in a dead end condition. |
| A\* | Based off quality of heuristic | Based off quality of heuristic | Yes | Yes with heuristic conditions | Priority Queue |  |
| Recursive Best First Search |  | Based off quality of heuristic | Yes | Yes if heuristic admissible | Stack |  |

Completeness above assumes the branching factor is **finite**.

**Iterative Deepening Depth First Search (also known as Iterative Lengthening Search)**

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| def ID\_DFS(problem, limit):  # Incrementally increase the maximum depth  for maximum\_depth in range(0, *limit*):  result = Depth\_Limited\_Search(*problem*.INITIAL\_STATE(),  *problem*, *maximum\_depth*)  # If solution found return it.  if(result is not None):  return result | def Depth\_Limited\_Search(*node*, *problem*, *depth*):  if(*problem*.GOAL\_TEST(*node*)):  return SOLUTION(*node*)  if(depth == 0):  return None  for *action* in *problem*.ACTIONS(*node*):  *child* = *problem*.RESULT(*node*, *action*)  *result* = Depth\_Limited\_Search(*child*, *problem*, *depth* – 1)  if(result is not None):  return result  return None |

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| **Space Complexity:** since at one time only keeping in memory at most d nodes. | **Time Complexity:** Depth-Limited-Search is called up to times. Each call to Depth-Limited-Search takes time.  Given: , Then | **Complete:** Yes since all nodes are explored if | **Optimal:** Yes if all steps have uniform cost. |

**Uniform Cost Search (Uniformed Search)**

Uniform cost search explores nodes on the frontier based of a monotonically increase cost function. Hence its evaluation function is:

also referred to as

**def** UCS(problem):

initial\_state = problem.**INITIAL\_STATE**()

priority\_queue = {}

explored\_set = {}

priority\_queue.enqueue(initial\_state)

# Continue until either a solution is found or all nodes explored.

**while**( len(priority\_queue) > 0):

node = priority\_queue.pop()

# Must only check AFTER dequeueing the item to ensure it is optimal.

**if**(problem.**GOAL\_TEST**(node)): return **SOLUTION**(node)

# Add the node to the explored set.

explored\_set.append(result)

**for** action **in** problem.ACTIONS(node):

result = problem.RESULT(node, action)

# If not in the priority queue then enqueue it.

**if**( result **not in** priority\_queue **and** result **not in** explored\_set):

priority\_queue.enqueue(result)

# Current version of node has lower cost than version in priority queue

**elif**( result **in** priority\_queue **and** result.COST() < priority\_queue[result]. COST()):

priority\_queue.remove(result)

priority\_queue.enqueue(result)

# No path found

**return** None

**Pseudo code for A\* and UCS is the same with the implementation of the COST() method.**

**A\* Algorithm**

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| A\* algorithm is a combination of the benefits of **Greedy-Best First Search** and **Uniform Cost Search**. | **Evaluation Function :**  Also written as: | Only performs the **GOAL-TEST** **after the node has been dequeued** from the priority queue. Similar to Uniform Cost Search. | Derives from Dijkstra’s Algorithm. |

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| **Example of A\* Performing Better**  **than Greedy Best First Search**  A-Star Perform Better Than GBFS.png  **Greedy Best First Search Oscillates Between Nodes A and B so it is Incomplete.**  **This graph is solvable by A\*.**  Greedy Best First Search is **memory efficient** since it does not need to remember where it has been. | **Example of DFS Performing Better than A\***  **DFS Perform Better than A-Star.png**  **Heuristic for A\* is Euclidean distance. In this case, A\* adds B then D to the frontier. It next expands B and adds C to the frontier. It next explores C and finds no solutions so it explores D then finds the goal.** |

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| **Recursive Best-First Search**  This algorithm is **optimal** when the heuristic is **admissible for trees**. The heuristic needs to be **consistent for tree search** to be optimal.  **f\_limit/min\_eval\_func\_val** – **Best alternative path available from the any ancestor of the current node.**  **Simplified Description of Recursive Best First Search**  1. Start from initial state and set the initial minimum cost of  2. Generate all successors of current node. Set successor cost to either current node evaluation function value () or the successors evaluation function cost.  3. Select successor node with minimum evaluation function () cost.  4. If current node is a goal state, then return the solution.  5. If this cost is more than the current minimum, backtrack to find node with current minimum.  6. Extract the evaluation function cost () of the second best successor of the current node.  7. Recurse using best successor found in step #3 and the minimum of the current minimum cost that was passed to the function and the second best successor of this node. This function results either a solution or None and updates the current best node’s evaluation function cost ().  8. If step #7 returned a solution, then return that, otherwise, jump to step #3. | **def** **RECURSIVE\_DEPTH\_FIRST\_SEARCH**(problem):  **return** **RDFS**(problem, problem.**INITIAL\_STATE**(), **inf**)  # Continues to recurse until current best cost is more than  **def** **RBFS**(problem, state, min\_eval\_func\_val):  # Check if a goal was reached. If so, return it.  **if**( problem.**GOAL\_TEST**(state) )**:**  **return** **SOLUTION**(state)  # Get set of successors  **for** a **in** problem.**ACTIONS**(state):  successors.**append**(problem.**RESULT**(state, a))  # Check a successor exists  **If**(len(successors) == 0)**:**  **return** **None**,  # Update all successor eval function values  **for** s **in** successors**:**  s.eval\_func\_val = **max**(node.eval\_func\_val, s.g + s.h)  **while**(True):  # Best successor is a node with min eval cost from successors  best\_successor = *node with least eval function value from the* ***successors***  # If the best successor is not better than current best, backtrack to current best  if(best\_succesor.eval\_func\_value > min\_eval\_func\_value):  **return None**, best\_successor.eval\_func\_value  # May need to recurse back to current level so store second best value for this level.  second\_best\_successor\_eval\_func\_val = *Eval func value for second best successor of state*  # Run RBFS again from current node with the new min value the minimum of the current  # minimum and the second best successor (i.e. alternative) for this current state/node.  result, best\_successor.eval\_func\_val = \  RBFS(problem, best\_successor, min(min\_eval\_func\_val,  second\_best\_succesor\_eval\_func\_val)  # If solution found, return it.  **if**(result **is not** None)**:**  **return** result |

**Memory Bounded Heuristic Search**

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| **Iterative Deepening A\* (IDA\*) Algorithm**  Variant of the A\* algorithm that ***generally* slower but uses less memory.** Sets a maximum total cost (i.e. ) to a starting value of . In each round, any node whose total cost (i.e. ) is greater than the maximum is ignored. Perform A\* for thresholds:  def IDA\_Star(problem, initial\_max\_cost, maximum\_cost):  current\_max\_cost = initial\_max\_cost  while(current\_max\_cost < maximum\_cost):  result = A\_Star\_Search(problem, current\_max\_cost)  if(problem.**GOAL\_TEST**(result)):  return result  current\_maximum\_cost += initial\_max\_cost  return None | **Simplified Memory Bounded A\***  Approach to save memory in A\* algorithm.  **Procedure:**   1. Perform A\* until you run out of memory. 2. Delete fringe or explored set node with the worst cost. |

**Heuristic Classification**

**Evaluation Functions for Three Related Search Algorithms:**

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| **Uniform Cost Search:** | **Greedy Best First Search:** | **A\* Search Algorithm:**  A\* algorithm is the only one of the three whose evaluation function estimates the cost of the **total solution.** |

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| **Admissible (Optimistic) Heuristic:** Any heuristic that never over estimates the cost of a solution. | **Consistent (Monotonic) Heuristic:** For every node, *n*, every successor, *n’*, that is reached by action, *a*, then the cost to reach the goal from *n* is less than or equal to the actual cost to go from *n* to *n’* by action *a* () plus the heuristic cost of *n’*.  **Note:** Any heuristic that is consistent is also admissible.  **Example:** Triangle Inequality when the heuristic is straight-line distance. |

**The tree-search version of A\* (i.e. DAG) is optimal if h(n) is admissible, while the graph search version of A\* is optimal if h(n) is consistent.**

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| **Lemma #1**  If was a consistent heuristic, then the values of are nondecreasing.  **Given a node *n*’ is a successor of *n* through action a, then:**  If *h(n)* is consistent, then:  Then: | **Lemma #2:** Whenever A\* selects a node for expansion, the optimal path to that node has been found.  Had lemma #2 not been the case, then there would have been another node *n’* on the path from the start to *n* that would have been on the optimal path.  **Because is non-decreasing, this node would have had a lower value of and would be expanded before *n* in A\*. Hence, this is a contradiction.** | **Combining Lemma #1 and Lemma #2**  **By Lemma #2:** If a goal node is explored, it is the optimal path to that goal node.  **By Invariant of A\*:** A\* algorithm explores nodes in non-decreasing order of .  **By Lemma #1:** is nondecreasing.  Combining Lemma #1, Lemma #2, and Invariant of A\*: Paths to any other unexplored states, including goal states, will have evaluation function values () greater than the first one explored. Hence, the optimal path to the first explored goal state is the optimal solution to the entire problem.  Since by lemma #2 A\* returns the optimal path to the first goal state, it returns the optimal path to the entire problem. |

**Choosing a Heuristic**

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| **Effective Branching Factor (*b*\*):** For a set of *N* moves, it is the equivalent number of uniform branches for a depth *d*. It is a way to quantify the quality of a heuristic.  Derives from:  **Best branch possible factor is 1.** | **Relaxed Problem:** A version of the actual problem with fewer restrictions.  An exact solution to a relaxed problem is an admissible heuristic for the original problem. | **Dominating Heuristic:** A heuristic that always has a lower branching factor than another heuristic.  **Composite Heuristic:** Given a set of **admissible** heuristics { none of which is dominating, then the best heuristic is the composite heuristic: |  |

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| **Subproblem:** A reduced version of the actual problem. Admissible heuristics can be derived from the solution to subproblems. | **Pattern Database:** Stores the exact solution for all versions of a particular subproblem.  To determine the heuristic cost for a version of the subproblem, look up the solution in the database and calculate the heuristic cost. | **Disjoint Patterns:** A problem can be divided into disjoint (i.e. nonoverlapping) subproblems. The disjoint solution to the problem is referred to as a disjoint pattern. | **Disjoint Pattern Database:** Stores solution to disjoint (non-overlapping, non-dependent) subproblems.  Using multiple disjoint subproblems in a disjoint pattern database, you can come up with a composite heuristic by **summing** the cost to solve each individual subproblem. |

**Local Search**

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| **Local search** generally operates using a single **current node** and generally moves to neighbors of that node. | If the local search problem is an **optimization problem**, then it is accompanied by an **objective function** that is to be maximized or minimized. | **Complete Algorithm:** Always finds a solution if it exists.  **Optimal Algorithm:** Always finds a global maximum or minimum. | **State Space Landscape:** Landscape has a location (i.e. state) and an elevation (utility from the objective function) |

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| **Hill Climbing Algorithm**  Local search algorithm that always proceeds to the next successor state with maximum utility. If two successors have the same utility, algorithm randomly chooses between them. Susceptible to **local maxima**.  Also referred to as **Greedy Local Search**.  **Variants of Hill Climbing**  **Sideways Move:** Allow hill climbing algorithm to move to a state of equal value. Helps to move past flat area in a graph. However, in a plateau, it can lead to an infinite loop so a limit on the number of consecutive sideways moves is common.  **Stochastic Hill Climbing:** Choose a successor state at random with the probability each successor is selected proportional to its utility.  **Hill Climbing with Restarts:** Hill climbing runs from a randomly chosen initial state. If it gets a solution, it returns. Otherwise, it generates another random initial state and repeats the process. Repeated *n* times or until a solution is found.  **Example:** If the probability of finding a solution from an initial state is ***p***, then it is expected  **restarts** will be required.  See page 122. | def HILL\_CLIMBING\_WITH\_RESTART(problem, max\_restarts):  while( max\_restarts > 0 ):  max\_restarts -= 1  problem**.INITIAL\_STATE** = problem.**RANDOMIZE\_STATE()**  result = Hill\_Climbing(problem)  if(problem.**GOAL\_TEST**(result)):  return result  return None  def HILL\_CLIMBING(problem):  current\_state = problem.**INITIAL\_STATE**()  while( True ):  # Update the previous utility  best\_successor = None  # Iterate through set of possible actions  for action in state.**ACTIONS**():  new\_state = problem.RESULTS(state, action)  if(best\_successor is None  or problem.**UTILITY**(new\_state) > problem.**UTILITY**(current\_state)):  best\_successor = new\_state  # Determine if the best successor is better than the current state  if(problem.**UTILITY**(best\_successor) > problem. **UTILITY**(current\_state)):  current\_state = best\_successor  else:  return current\_state  return None  **Note: This is a goal based version of Hill Climbing. If you are simply searching for a maximum or minimum, you would need to modify the algorithm to return “current\_state” at the end.** |

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| **Simulated Annealing**  Can be used for either maximization or minimization problems.  Algorithm is designed to allow the current\_node to move to a worse state with decreasing probability as time progresses.  Probability of Moving to a Lower Value Solution is:  Simulated annealing chooses **a random successor.** | import **math**  import **random**  def **SIMULATED\_ANNEALING**(problem, schedule, limit, t\_min):  current\_state = problem.**INITIAL\_STATE**()  t = 0  while( True ):  t += 1  T = **schedule**(T)  if(T < t\_min or problem.**GOAL\_TEST**(current\_state)):  return current\_state  # Get the set of actions.  actions = current\_state.**ACTIONS**()  # If no successors possible, terminate  if(len(actions) == 0):  return None  # Randomly select a successor  a = actions[random.randint(0, len(actions) – 1]  # Get the successor state  next\_state = problem.**RESULT**(current\_state, a)  # Calculate the error  error = problem.**UTILITY**(next\_state) - problem.**UTILITY**(current\_state)  # If error is positive or probability less than specified number, then update the current state.  if(error > 0 or random.random() < math.exp( error/ T):  current\_state = next\_state  **Note: This version of the code is a maximization problem. Would need to modify slightly for a minimization problem.** |

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| **Local Beam Search**  Type of local search.  **Procedure:**  1. Begin with *k* randomly generated states.  2. Check if any descendent states at the goal. If so, return state.  3. Order all successors from the *k* states and sort them by decreasing performance.  4. Choose the best *k* successors. If any successor has performance measure better than the current best, return to step #2.  The *k* successors are considered a **pool of candidates**. The successors are considered **offspring**. | **Variant of Local Beam Search**  Stochastic Local Beam Search: Choose *k* successors stochastically based off some metric. |

**Genetic Algorithm**

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| A genetic algorithm is a **stochastic beam search** algorithm with one key modification:   * In local beam search, successors come from **modifying a single state (asexual reproduction)**. * In genetic algorithm, successors come from **combing two parent states (sexual reproduction)**.   **Population**: Set of *k* solutions. The **initial population** is *k* randomly generated solutions.  **Individual:** One solution/state in the population.  **Fitness Function:** Evaluation function that rates the quality (i.e. fitness of a solution) generally with general condition that better states have higher fitness function value.  **Crossover:** Process of merging two solution states to form a new successor.  **Mutation:** Random change to a successor solution. | **def** **GENETIC\_ALGORITHM**(problem, *FITNESS\_FUNCTION*, t\_max)  # Generate the population.  population = problem.**GENERATE\_POPULATION**()  # Start at time 0.  t = 0  **while**(t < *t\_max* **or Not** problem.**GOAL\_TEST**(best\_solution))**:**  # Increment current time.  t += 1  new\_population = {}  best\_solution = None  **for** i **in** range(0, problem.**POPULATION\_SIZE**())**:**  # Select two parent solutions.  x = **RANDOM\_SELECTION**(population, *FITNESS\_FUNCTION*)  y = **RANDOM\_SELECTION**(population, *FITNESS\_FUNCTION*)  # Merge the two solutions  child = **REPRODUCE**(x, y)  # Mutate on a low probability  **if**(random.random() < problem.**MUTATION\_PROBABILITY**)**:**  problem.**MUTATE**(child)  **if**(best\_solution **is None or** problem. **UTILTY**(best\_solution) < problem.**UTILTY**(child))**:**  best\_solution = child  # Add the child solution to the new population.  new\_population.**append**(child)  # Set the population to the newly created set.  population = new\_population  **return** best\_solution  **def REPRODUCE**(x, y):  # Pick a random cross over point  crossover\_point = **random.randint**(0, len(x) – 1)  # Crossover the two halves  **return** x[0:crossover\_point] + y[crossover\_point:len(y)] |

**8-Puzzle Goal State:**

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| **X** | 1 | 2 |
| 3 | 4 | 5 |
| 6 | 7 | 8 |

**Minimax (Adversarial Search)**

**Adversarial search** **problems** are those search problems that arise in **multiagent**, **competitive** environments. Adversarial search problems are also known as **games**.

In a **zero-sum game**, the results for the two players are always **equal and opposite**.

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| **Optimal Strategy** – A sequence of contingent decisions that will lead to outcomes as least as good as any other sequence of decisions against an infallible player. | **Perfect Information** – Any situation where an agent has all relevant information with which to make a decision and the results of actions are **deterministic**. | **Minimax Value** – Utility of being in a current state assuming both players play optimally until the end of the game. |

**Initial State** in Minimax – *s0*

Given a state, *s*, the six key methods used on that state are:

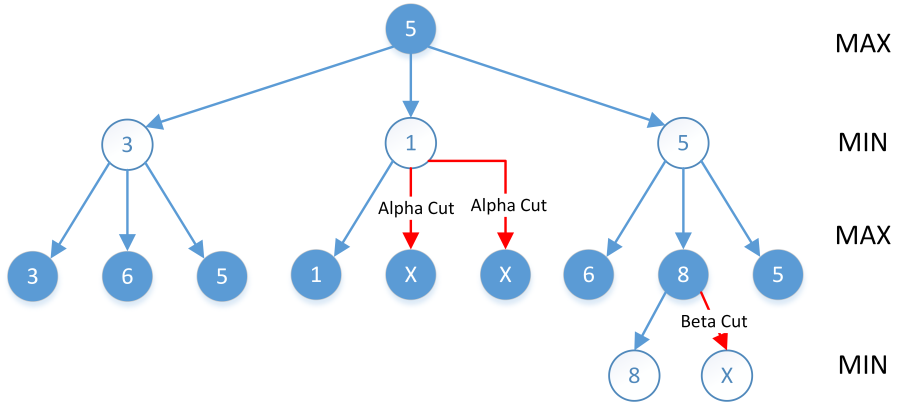
1. PLAYER(s) – Returns active player for the current state
2. ACTIONS() – Set of all possible actions/moves that can be made.
3. RESULTS(s,a) – Given a state, *s*, and an action *a*, it returns the successor state. It is also called a **Transitional Model**.
4. CUTOFF\_TEST(s,d) – Used in Heuristic minimax. Given a state, s, and a recursive depth, d, it determines if the cutoff condition of either a maximum depth or goal state has been reached.
5. TERMINAL\_TEST(s) – Used in standard minimax. Given a state, *s*, this function returns whether a goal state has been met. **Terminal states** are **leaf nodes** in the **search tree.**
6. UTILITY(s) – Given a state, *s*, this function returns the state’s utility score. It is also called a **Utility Function.**

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| **Time Complexity with Alpha-Beta Pruning:** | **Time Complexity without Alpha-Beta Pruning:** |

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| def **Minimax\_Algorithm**(state, is\_max):  alpha\_max = -inf  beta\_min = inf  best\_successor = None  # Iterate through all possible actions from this state  for *a* in state.**ACTIONS**():  # Get the successor state  next\_state = state.**RESULT**(state,a)  # Call heuristic minimax with starting depth 0  score = **H-Minimax**(next\_state, 0, !is\_max,  alpha\_max, beta\_min)  if(is\_max and score > alpha\_max):  best\_successor = a  alpha\_max = score  elif(not is\_max and score < beta\_min):  best\_successor = a  beta\_min = score  # Return the move with the best score  return best\_move | def **H-Minimax**(state, depth, is\_max, alpha\_max, beta\_min)  # *p* is the reference player for the utility function. Typically max.  if ( state.CUTOFF-TEST(depth) ):  return state.UTILITY(p)  for a in state.ACTIONS():  next\_state = state.RESULT(state, a)  if(is\_max):  # Perform beta pruning  alpha\_max = max(alpha\_max, H-Minimax(next\_state, depth+1,  not is\_max, alpha\_max, beta\_min))  if(alpha\_max ≥ beta\_min):  return alpha\_max  else:  beta\_min = min (beta\_min, H-Minimax(next\_state, depth+1,  not is\_max, alpha\_max, beta\_min))  # Perform alpha pruning  if(alpha\_max ≥ beta\_min):  return beta\_min  # After all actions tested, return score.  if(is\_max):  return alpha\_max  else:  return beta\_min |

**Alpha Beta Pruning**

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| **Alpha (α)** – Maximum value found along the path by the MAX player.  **Alpha Cut/Alpha Pruning** – Performed by the **MIN player**. When the MIN player’s minimum score is already less than a previous MAX player’s maximum score, stop investigating subsequent paths and return the **current minimum score**. | **Beta (β)** – Minimum value found along the path by the MIN player.  **Beta Cut/Beta Pruning** – Performed by the **MAX player**. When the MAX player’s maximum score is greater than a previous MIN player’s minimum score, stop investigating subsequent paths and return the **current maximum score**. |



**Minimax Search Tree Example with Alpha and Beta Cuts.**

This is a three move/**ply** search tree.

**Constraint Satisfaction Problem**

**Search problems** deal with states that are **atomic** (i.e. indivisible).

Often a state has field variables. Such field values are called a **factored representation** of the problem. A state **solves** a factored representation if each field variable satisfies all constraints on that variable.

**A factored representation can allow you to eliminate large areas of the search space by identifying then ignoring variable/value combinations that violate constraints.**

A constraint satisfaction problem **solution** is an assignment of values to variables that satisfies all constraints.

Assignment of values to variables in CSPs is **commutative**. Hence, the order that the values are assigned do not matter. If you consider the problem a search tree, there are at most *d* children from each node leaving a total of solutions for a finite domain

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| **Components of a Constraint Satisfaction Problem:**   1. **– Set of variables** 2. **– Set of Domains** 3. **– Set of Constraints**   **Optional Definition:**  - Relation of multiple variables | **Definition of a Constraint**  A constraint is a pair:  **Scope:** Tuple of variables that participate in the constraint  **Relation:** A relation that the variables can take on. |

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| **Assignment** – Allocation of values to variables.  **Solution:** A complete and consistent assignment. | **Consistent Assignment** – An assignment of values that does not violate any constraints.  This leads to the term **consistency** which is the **satisfaction of constraints.** | **Complete Assignment** – Every variable is assigned a value. | **Partial Assignment** – Only a subset of variables are assigned a value. |

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| **Domain**  A variable’s domain can be either **discrete** or **continuous**. If it is discrete, it can be either **finite** or **infinite** (e.g. set of integers).  **Simplest CSP Type:** Finite, discrete domain | **Constraint Language**  Defines the allowed relations between variables. It eliminates the need to enumerate allowed value lists. | **Linear Programming Problem:** Continuous CSP with **linear constraint function**(s).  Constraint functions can also be **nonlinear**. |

**Constraint Types**

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| and  **Example Constraint:**  with | **Precedence Constraint:** A constraint that forces one variable to occur before (i.e. be less than) another variable.  **Example:** | **Disjunctive Constraint:** A constraint that two variables do not overlap (i.e. are not equal):  **Example:**  or | **Absolute Constraint:** Any constraint that must be met. | **Preference Constraint:** A constraint which guides the solution to preferred values.  Problems that optimized preference constraints are called **constraint optimization problems**. |

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| **Unary Constraint** – A constrain involving only a single variable. | **Binary Constraint** – A constrain involving exactly two variables. | **Higher Order Constraint:** A constraint that involves a **fixed** number of variables that is more than two.  **All higher order constrains can be reformed as a set of binary constraints.** | **Global Constraint:** A constraint that takes an **arbitrary** number of variables. It does not need to be all variables. It just needs to be **not fixed** (i.e. arbitrary).  **Example:**  ***Alldiff*** |

**Constraint Graph/CSP Network:** Representation of a CSP as a graph. Each node is a variable and the arcs are binary constraints.

**Inference:** Using known/assigned values for a set of variables to select the values for other variables.

**Constraint Propagation:** Using the constraints to reduce the number of legal values for a variable. This in turn reduces the number of legal values for other variables in a cycle.

**Local Consistency:** Given a constraint graph, enforcing consistency (i.e. ensuring variables satisfy constraints) locally **in each part of the graph** leads to invalid values being eliminated throughout the graph.

**Node Consistency**

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| **Node Consistent Variable** – Any variable where every value in the variable’s domain **satisfies all of its unary constraints** in a CSP network. | **Node Consistent Network** – Any CSP network where **all variables are node consistent**. | Node consistency can be done as a **preprocessing step** to eliminate invalid values. |

**Arc Consistency**

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| **Arc Consistent Variable** – Any variable where every value in the variable’s domain **satisfies all of its binary constraints** in a CSP network.  Variables are arc-consistent with respect to one another. Example: X being arc consistent with respect to Y does **NOT** imply Y is arc consistent with respect to X. | **def** AC\_3(csp):  arc\_queue = []  # Add all binary constraints to the queue.  **for** b\_constraint **in** csp.BINARY\_CONSTRAINTS**:**  arc\_queue.append( (b\_constraint.X\_i, b\_constraint.X\_j )  # Iterate until all arcs have been made consistent or an inconsistency is found.  **while**( len(arc\_queue) > 0 )**:**  (X\_i, X\_j) = arc\_queue.pop()  # Check if the domain of X\_i is revised.  **if**( REVISE(csp, X\_i, X\_j) )**:**  **if**(len(X\_i) == 0 )**:**  **return** **False**  # Only X\_i’s domain is reduced in function “REVISE” so only check relative to that.  # Since X\_i’s domain is reduced, any variable that is constrained by X\_i may need to be reduced  **for** X\_k **in** X\_i.NEIGHBORS() – {X\_j}**:**  # Only add back to domain if not X\_j  **if**(X\_k != X\_j **and** (X\_k, X\_i) not in arc\_queue):  arc\_queue.append( (X\_k, X\_i) )  **return** **True**  **def** REVISE(csp, X\_i, X\_j):  revised = False # Confirmed in loop  # Verify all elements in the domain of X\_i have a corresponding value in X\_j.  **for** x **in** csp.D\_i:  constraining\_value\_exists = False  # Iterate through all elements in X\_j’s domain to see if it constrains x in X\_i.  **for** y **in** csp.D\_j:  **if**( (x,y) **in** csp.C(X\_i, X\_j)) **:**  constraining\_value\_exists = **True**  **break**  # If no constraining value exists in X\_j, then remove the value from X\_i.  **if**(not constraining\_value\_exists)**:**  csp.D\_i.remove(d)  revised = **True**  # Return whether the domain of X\_i was revised (i.e. reduced)  **return** revised  Page 209 |
| **Arc Consistent Network** – Any CSP network where **all variables are arc consistent**. |
| **AC-3 (Arc Consistency Algorithm #3)**  Algorithm used to solve for Arc consistency  Only possible with finite domains. |
| **Constraints in Arc Consistency Algorithm**  In each iteration of AC-3 algorithm, it only checks the variable being arc-constrained (example in constraint (X,Y), X is being constrained by Y). To have a two directional constraint for X and Y, arc queue would need to contain (X, Y) and (Y, X)  After reducing the domain of X from constraint (X, Y), algorithm needs to recheck any domains that were constrained by X to ensure its domain values are still valid. |
| **Running Time of AC-3 Algorithm**  1. **REVISE Function**:  For each value in the domain of (up to *d* elements), you iterate overall elements in the domain of . Hence the running time is:  2. **Number of Times REVISE function is Run Per Constraint:**  The REVISE function is run whenever a constraint is popped off the queue. If the domain size is queue, it can be popped off the queue up to *d* times (once for each element.  3. **Number of Constraints:** *c*  **Total Running Time:** |

**Path Consistency**

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| **Path Consistency** – **A two variable set are path consistent with respect to a third variable**  if for every assignment of values to and consistent with the constraint , there is a valid assignment to that satisfies the constraints and . | **Origin of the Term “Path Consistency”**  Given a two variable set that is path consistent with respect to a variable , then it is like is on the path between and . | **Algorithm to Solve to Check for Path Consistency:** PC-2 |

**k-Consistency**

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| A CSP is ***k*-consistent** if for **any set of *k-1* variables** and for **any consistent assignment** to those variables, a consistent value can **always** be assigned to any *k­*-th variable.  **Proving *k*-consistency takes exponential and space in the worst case**. | **1-consistency** is **node consistency.**  **2-consistency** is **arc consistency**. | **Strongly *k*-consistent:** Any CSP that is 1-consistent and 2-consistent and 3-consistent through k-consistent. Hence it is consistent for variable sets of size 1 through *k*. | Given *n* variables and a CSP that is strongly *n*-consistent, then an assignment of values is possible for this CSP.  **Running Time to Solve *n*-Consistent CSP**  **Time Complexity:**  Running time derives since for every *i*-th variable to assign, you must check all *i-1* variables for every *d* elements in the domain. Hence: |

**Consistency Checks for Global Constraints**

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| **Global Constraint** – A constraint with an arbitrary number of variables.  **Example Global Constraint:** *Alldiff* | **Alldiff Consistency Algorithm**  1. Delete a variable that has a singleton domain.  2. Remove the value from the domains of all other variables.  3. If any singleton domain variables still exists, jump to step #1.  4. If a domain has no values or there are more values than there are variables, the *Alldiff* constraint fails. | **Simplified Explanation of Alldiff Consistency Check**  If there are *m* variables and *n* possible values and  , then an inconsistency exists. |

**Sudoku**

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| Square grid of *n* by *n* cells. All numbers in a row must be unique and all numbers in a column must be unique. For every by subgrid, all numbers must be unique. Each section of the board where all numbers must be unique (e.g. row, column, subgrid) is called a **unit**.  **Formal Definition of Sudoku as a CSP:**  **Variables:**  total variables (one for each cell).  **Domain:**  **Constraints:** *Alldiff* constraints for each unit.  AC-3 Algorithm can be used to infer the value of cells and to reduce the domains of cells. |

**CSPs and Backtracking**

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| **Backtracking Search** – Variant of Depth First Search where values are assigned to variables until no consistent, legal assignments are possible for a given variable at which point the algorithm ***backtracks*** to try to reassign a previous variable to a new value. | **def BACKTRACKING\_SEARCH**(csp):  **return** BACKTRACK({}, csp)  **def BACKTRACK**(assignment, CSP):  # Consistency of all variable assignment checked so if assignment is complete, it is a solution.  **if**(csp.**COMPLETE\_ASSIGNMENT**(assignment)) **return** assignment  # Select the next variable to assign  next\_var = csp.**SELECT\_UNASSIGNED\_VARIABLE**()  # Order the domain values based off which want to check first  var\_doman = csp.**ORDER\_DOMAIN\_VARIABLES**(assignment, next\_var)  # Iterate through all domain values.  **for** d **in** var\_domain:    # Ensure the assignment is consistent.  **if**(csp.**CONSISTENT\_ASSIGNMENT**(assignment, *d*))**:**  # Add the variable value to the assignment  assignment[var\_domain] = d    # Get and apply any inferences  inferences = csp.**INFERENCE**(assignment)  # Only recurse if valid inferences found.  **if**(inferences **is** **not** **None**)**:**  assignment.**APPLY\_INFERENCES**(inference)  result = **BACKTRACK**(assignment, csp)  **if**( result **is** **not** **None**):  **return** result  assignment.**REMOVE\_INFERENCES**(inference)  # Since no solution found using this assignment and variable value  # remove this variable value from the assignment.  **remove**( assignment[var\_domain] )  # No solution found so return None for failure.  **return** None |
| **Key Functions in Backtracking Search**  1. **SELECT\_UNASSIGNED\_VARIABLE**  2. **ORDER\_DOMAIN\_VALUES**  3.  **INFERENCE**  4. **BACKTRACK** (recursion) |
| **See page 215.** |

**Making Backtracking Search More Efficient and Sophisticated**

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| **Variable Ordering**  By selecting a **variable most likely to fail earliest,** you are **prune the search tree** and **reduce the effective branching factor**.  **Minimum Remaining Value (MRV), Fail First,**  **Most Constrained Variable Heuristic:** Select the variable to assign next that has the smallest inferred domain (i.e. least remaining legal values).  **Degree Heuristic:** Select the variable for expansion that has the largest number of constraints on other variables. **Most commonly used heuristic to select the first variable for assignment.**  Degree heuristic can be used as a **tie breaker** for the more powerful MRV heuristic. | **Value Ordering**  **Least-Constraining Value Heuristic:** Select the value that rules out the least number of values for neighboring variables in the graph. | **Interleaving Search and Inference**  AC-3 can be used to infer reductions in the search domain both **before and during search**.  **Forward Checking** – One way to implement “Inference” in Backtracking algorithm. Whenever a variable is assigned, establish arc consistency for it on all unassigned variables. If arc consistency checking was done in preprocessing, forward checking adds no value.  MRV can be combined with forward checking to further prune the search tree. | **Chronological Backtracking:** Simplest form of backtracking. **Revisit the last assigned variable** (i.e. **most recent decision**) before the current variable. If the previous variable does not constrain the current variable, backtracking to only that level is wasteful.  **Intelligent Backtracking**  Better to backtrack to a variable that may fix the consistency issue.  **Conflict Set:** Set of value assignments that conflict with a some value for a variable. **Note:** This is value assignments not variables since a variable that can conflict for one value does not conflict for the currently assigned value.  **Backjumping:** Backtracking to the most recent variable in the conflict set. |

**Variable ordering is fail-first** ordering while **value ordering is fail-last**. This is because when you are trying to fail-first by selecting a variable, the order you inspect the values does not matter as you need to **inspect them all anyway**. As such, it makes the most sense to inspect the best solutions first in case one of them ***does actually succeed***.

**Logical and Knowledge Based Agents**

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| **Knowledge Base (KB)** – Central component of a knowledge based agent. Composed of a set of **sentences**. **Similar to a database.** | **def** KNOWLEDGE\_BASED\_AGENT()  # KB is the persistent knowledge base.  # t a time counter initially starting at 0.  **TELL**( KB**, MAKE\_PERCEPT\_SENTENCE**(t) )  action = **ASK**(KB, **MAKE\_ACTION\_QUERY**(t) )  **TELL** ( KB, **MAKE\_ACTION\_SENTECE**(t) )  t += 1 # Increment time  # Return the selected action.  **return** action |
| **Knowledge Representation Language** – Formal notation used to express sentences in the knowledge base (KB). |
| **Sentence** – Statements that define the knowledge based. They have a specific notation called a syntax and their value (i.e. true or false) is defined by the semantics. |
| **Axiom** – A sentence that is taken as given without being derived from other sentences. |
| **Inference** – Deriving new sentences from existing sentences. |
| **Valid Knowledge Base Operations:**   1. **TELL** 2. **ASK**   **Supporting Knowledge Based Agent Commands:**   1. **MAKE\_PERCEPT\_SENTENCE** 2. **MAKE\_ACTION\_QUERY** 3. **MAKE\_ACTION\_SENTENCE** |
| **Background Knowledge** – Initial knowledge in the knowledge base. |
| **Four Step Procedure for a Knowledge Based Agent:**   1. **Tell the knowledge base what it perceives.** 2. **Ask the knowledge base it should perform.** 3. **Tell the knowledge base the action it will perform.** 4. **Executive the action.** |

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| **Knowledge Level** – What the agent knows at a give point in time.  Given an agent’s knowledge level and goals, you can predict its actions. | **Declarative Approach** – Tell the knowledge base all it needs to know. | **Procedural Approach** – Procedures for desired behaviors and actions are hard coded into the agent. |

**Wumpus World**

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| The knowledge based agent is in an environmentconsisting of rooms connected by passageways. Some rooms contain bottomless pits while others contain goal. One wumpus lives in the cave in one room. Wumpus eats anyone who enters its room but does not move. Player has one arrow that can kill the wumpus. | **Performance Measure**  +1000 points for getting gold.  -1000 points for falling into a pit or eating a wumpus.  -1 for each action taken.  -10 for using an arrow. | **Actuators**  Move forward one room.  Turn left 90 degrees.  Turn right 90 degrees.  Shoot the arrow  Climb out (if in starting space) | **Sensors**  **Stench:** A wumpus is in an adjacent room.  **Breeze:** A pit is in an adjacent room.  **Glitter:** Gold is in the player’s room  **Scream:** Wumpus is killed.  **Bump:** Player walks into a wall. |

**Logic**

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| **Syntax** – Sentence formatting to make all knowledge sentences well formed. | **Semantics** – Provide meaning to sentences. It defines **truth** for every **possible world**.  **Example:** For the sentence, is true in the world where and . | **Model** – Substitute for the phrase “**possible world**.” **A model fixes the truth or falsehood for every relevant sentence.** | **Satisfaction:** Making a sentence true using an allowed model/possible world.  **Example:** If sentence *α* is true in model *m*, then model *m* **satisfies** sentence *α*. |

**Entailment**

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| **Entailment Between Sentences: When one sentence logically follows from another sentence or set of sentences. It is similar to implies in philosophy.**  **Symbol:**  Given two sentences *α* and *β*, then sentence *α* entails the sentence *β* if and only if:  The knowledge base is a set of sentences. The knowledge base is false in models that conflict with the knowledge base. | **Model Checking:** Given a knowledge base, KB, and verify it is a model of *α*. Hence:  **Model checking entails enumerating all possible models to determine whenever *KB* is true that *α* is also true. It only works on finite domains.**  **Logical Inference:** Process of drawing conclusions (i.e. new sentences) through entailment.  **Symbol of Inference:** ˫  Given a knowledge base, *KB*, and a sentence *α*, if an inference algorithm, *i*, inferred *α* from *KB* then: | **Sound or Truth Preserving Inference Algorithm:** Can only derive entailed sentences. **Hence it cannot prove any sentence that is wrong.**  **Example:** Model checking is a sound algorithm since it does not work on infinite spaces.  **Complete Inference Algorithm:** Can derive any entailed sentence. **A complete inference algorithm can prove anything that is right.** |

**Syntax**

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| **Syntax:** Defines allowable sentences.  **Semantics:** Defines what a sentence means.  **Model:** Fixes the **truth value** (i.e. true or false) for each proposition symbol.  **Atomic Sentence:** Simplest type of sentence and contains a single **propositional symbol** (i.e. **variable**)  **Propositional Symbol:** Represents a proposition or statement that can be either true of false.  **Naming Convention:** First letter is capitalized followed by lower case letters and subscripts.  **Positional symbols with fixed meaning:** True (always true position) and False (always false proposition) | **Logical Connectives**  Symbols that operate on propositional logic symbols.  : Not (**Negation**)  : Or (**Disjunction**). Individual terms are called **disjuncts**.  : And (**Conjunction**). Individual terms are called **conjuncts**.  : Imply (**Implication**)  or : **Biconditional.** “**If and only if**”  **is True unless *A* is true and *B* is false. is true only if A and B are both true or are both false.**  If , then:   * A is the **premise** or **antecedent** * B is the **conclusion** or **consequent**. | **Valid Sentence**  **Operator Precedence**  , , , , |

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| **Inference Proving**  Checking if | |
| **Model Checking:** Enumerate all the models and check if all for all possible models where KB is that is also true.  **Model checking is very similar to a truth table.** | **Theorem Proving:** Using sentences already in the model, apply rules of inference to construct a proof of the desired sentence without consulting models. |

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| **Literal:** In a complex sentence, a literal is either an atomic sentence (i.e. **positive literal**) or its negation (i.e. **negative literal**). | **Logical Connectives:** Used to construct complex sentences out of atomic sentences. |

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| **Logical Equivalence:** Two sentences and that are true in the same set of models.  **Notation:** | **Validity**: A sentence that is **valid** (**true**) in **all models**.  **Tautology**: A valid sentence. |

**Common Logical Equivalences**

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| **Commutative of** |  | **Commutative of** |  |
| **Associativity of** |  | **Associativity of** |  |
| **Double Negation** |  | **Contraposition** |  |
| **Implication Elimination** |  | **Biconditional Elimination** |  |
| **DeMorgan’s Law** |  | **DeMorgan’s Law** |  |
| **Distributivity of and** |  | **Distributivity of and** |  |
| **Modus Ponens** |  | **Modus Tollens** |  |
| **And Elimination** |  |  |  |

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| **Satisfiability:** A sentence that can be made true with some model. For a finite environment, satisfiability can be by enumerating all possible models and seeing if any leads to the statement being true. CSP consistency checking is a type of satisfiability problem.  **Example:** is true in the model: | **Validity and Satisfiability:** A sentence is valid if and only if its negation is not satisfiable.  **Reduction ad absurdum/Proof By Reduction/Proof by Contradiction**: Given a logical expression, assume the opposite of the expression and determine if it is satisfiable. |

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| **Proof:** A chain of conclusions that leads to the establishing some statement following from the knowledge base. |

**Example**

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| Consider a situation where four light switches on a control panel. Define a knowledge base for this system with conditions defined in **Part A** and **Part B**.  **Definition:**  : Propositional symbol for the first switch and is true if the switch is on and false otherwise.  : Propositional symbol for the second switch and is true if the switch is on and false otherwise.  : Propositional symbol for the third switch and is true if the switch is on and false otherwise.  : Propositional symbol for the fourth (i.e. last) switch and is true if the switch is on and false otherwise. | **Part A:** The first and last switches are never both on.  **Part B:** At least one switch must be on. |

**Python Review**

**Python Basics**

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| **Command Line Call to Run Python:**  *python filename.py*  **Python File Extension:**  \*.py | **Command to Print to Console:**  *print "Hello World!”*  **Printing without Inserting a Newline:**  Use “,” (Comma)  *print* “Hello World”, | **Command to Get Last Result:**  \_ (Underscore)  **Example:**  >>> 2/3 + 7.9  >>> print \_ + 1 # prints 8.9 | **Valid Python Operators:**  +, \*, -, /, \*=, /=, -=, +=, %, ==, !=  // (Integer Division), \*\* (Power)  **Math Functions:**  *math.exp*( *value* ): e^value  *random.randint*(n,m): Integer n ≤ x ≤ m  *random.random*(): Float 0 ≤ x < 1  **Invalid Operators:**  ++, --  **Minimum and Maximum Value:**  inf, -inf |

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| **Conditionals:**  if( *expr* ):  # Do something  *elif*( *expr* ):  # Do something  *else*:  # Do something | **Boolean Arithmetic:**  *is*, *and*, *or*, *not*  **Boolean Literals:**  *True*, *False*  **Check Membership in List:**  *in* | **File IO:**  f = *open*(“filename.txt”, “w”)  line = f.*readline*()  f.*close*()  # Iterate over a file line by line  for line in open(“my\_file.txt”):  #Do something | **Formatted Printing:**  Use the % symbol similar to C/C++  *print* “%3d %0.2f” % (10, .9799)  # Prints “10 0.98” |

**Python String Manipulation**

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| **Python String Implementation**  Immutable ***list*** of characters.  **String Concatenation:**  + (plus sign) | **Converting from a String:**   * **int**(“38”) * **float**(“46.456”)   **Converting to a String:**   * **str**(7) * **repr**(32.9) | **Substring Manipulation**  Use [] like a list with the first character index 0  a = “Hello World”  *print* a[4] # Prints “o”  *print* a[:5] # Prints “Hello”  *print* a[6:] # Prints “World”  *print* a[3:8] # Prints “lo Wo” | **Checking for Substring:**  Use the *in* operator:  if( “hello” in “hello world”):  *print* “It’s in there.”  **Get Index of Substring:**  x = “hello world”.index(“llo”)  print x # Prints “2” |

**Element Containers**

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| **List (Array) Basics:**  Able to hold data of different types in the same list including other lists. Uses **[]**  x =[ 5, 4, “hello”, “world” ]  *print* x[1] # Prints “4”  *print* x[1:] # Prints “[4, “hello”, “world”]”  *print* x[0:2] # Prints “[4, 5]”  y =[ [3, 2], [1, 0]]  print y[1][0] # Prints 1 | **Nested (Two-Dimensional) Lists:**  y =[ [3, 2], [1, 0]]  *print* y[1][0] # Prints 1  **Concatenating Lists:**  x = [ 1, 2, 3]  y = [4, 5]  z = x + y  *print* z # Prints “[1, 2, 3, 4, 5]” | **List Length:**  Use **len**()  x = [1, 2, 5, 10]  *print* len(x) # Prints “4”  **Extracting List Properties:**  **max**( *list* ) – Gets Maximum Value in List  **min**( *list* ) – Gets Maximum Value in List | **Tuple:**  Immutable list. Created used **()** parenthesis.  **Accessing Tuple Elements:**  c = (4, 5)  print c[1] # Prints “5”  a, b = c # a = 4 and b = 5 |

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| **Creating a Tuple:**  a = (1, 2, 3) # Tuple of size 3  b = ( x, y ) # Tuple made of two variables  c = “Hello”, “World” # Tuple of size 2  d = () # Empty Tuple  e = “yo”, # Tuple of size 1  f = (“yo”, ) # Equal to e  g = (d, ) # Tuple of empty tuple ( (), ) | **Sets:**  Unordered collection of unique elements.  x = set( [ 3, 6, 9, 2])  my\_set = set(“goodness”)  print my\_set # Prints [“g”, “o”, “d”, “n”, “e”, “s”] with **no duplicates**  **Frozenset:**  An immutable set.  x = frozenset([4, 5, 6])  **Set Operations:**  | Union, & Intersection, - Difference,  ^ Symmetric Difference (XOR) | **Dictionary:**  Associative Array (i.e. hash table). Uses **{}** curly brackets.  person ={  “name”: “bob”,  “age”: “27”,  “sex”: “Male”  }  print person[“name”] # prints “Bob”  **Deleting from a Dictionary:**  **del** person[“name”] | **Dictionary Membership Test:**  Use the keyword “in”  if( “name” in person ):  *print* person[“name”] # Prints “bob”  **Accessing Tuple Elements:**  person.**keys**() # Gets all dict keys  person.**values**() # Gets all dict values  person.**len**() # Gets all dict length |

**Looping and Iteration**

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| **While Loop:**  while( *expr* ):  # Do something | **For Loop:**  for x in [2, 4, 5, 6, 9]:  *print* x  for y in range(1, 10):  *print* y # Only prints 9 lines | **range:**  Iterable object in Python.  *range*(0, 10) – Creates list of 0 to 9 in steps of 1  *range*(10) – Starting 0 not needed. Same as range(0,10)  *range*(0, 5, 2) – Starts 0 and steps by 2 until 5  *range*(7, 2, -1) – Starts at 7 and decrements by 1 until 3  **range vs. xrange:**  range creates an array that Python iterates over. This is memory inefficient. *xrange* acts like a real for loop without the memory overhead of range. | **Iterable Objects in Python:**  *set*, *frozenset*  List, Tuple  Dictionary *key*  File (*open*(“filename”)  String (letter by letter)  Generator |

**Functions**

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| **Creating a Function:**  **Keyword:** ***def***  def my\_func(*params*):  # Do something  **Keyword to Return:** **return**  **Supports Recursion:** Yes  **Taking an Arbitrary Number of Input Variables**  **Keyword: \*args**  **def** my\_function(**\*args**):  **pass** | **Scope:**  Default scope in python is **local**.  i = 5  **def** print\_i():  i = 4  print i  print\_i() # Prints “4”  print I # Prints “5” | **Keyword to Add to Global Scope: global**  **def** assign\_i():  global i  i = 3 | **Storing a Function in a Variable:**  **def** print\_i()  i = 4  print i  a = print\_i  a() # Prints “4” |

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| **Anonymous Function:**  Keyword: **lambda**  g = **lambda** x: x\*\*3  print g(10) # Prints “1000”  h = **lambda** y,z: z + 2\*y  print h(2, 3) # Prints “8”  **def** make\_adder(n):  return **lambda** z: z+n  f = make\_adder(2)  print f(3) # Prints “5”  print f(6) # Prints “8”  g = make\_adder(4)  print f(3) # Prints “7”  print f(6) # Prints “10”  **LAMBDA NEVER HAS A RETURN** | **Generator**  Uses the **yield** construct and the object method **next**.  Allows you to get a sequence of objects in a dedicated routine.  def countdown(n):  while(n > 0):  **yield** n  n -= 1  # Creates the function call as object but does NOT run it yet  x = countdown(3)  *print* x.next() # First runs “countdown(3)” then prints “3”  *print* x.next () # Prints “2”  *print* x.next () # Prints “1” | **Coroutine**  Uses the **yield** construct and the object method **send** and **next**.  Allows you to pass a sequence of values one at a time to a function (e.g. log file printer)  def print\_matches(text):  *print* “Trying to find text: “ + text  while(True):  line = **(yield)**  if(text in line ):  *print* line  # Creates the function call as object but does NOT run it yet  x = print\_matches(“hello”)  x.next() # Runs to first yield.  *print* x.send(“lalalala”) # Prints nothing  *print* x. send (“hello world”) # Prints “hello world” |

**Classes**

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| **class** **ClassName**(*inherited\_class1, inherited\_closs2*):  # Class variables  class\_name = “Class Name”  # Constructor  **def \_\_init\_\_**(self):  *self*.attribute1 = 1  *self*.attribute2 = [3, 4]  *self*.length\_value = 1  # Called without parenthesis for methosd  **@property**  **def** length(self)  **return** *self*.length\_value  # Called by ClassName.static\_method(*arg*)  **@staticmethod**  **def** print\_class\_name()  *print* class\_name  **Calling Supercass Methods**  **Option #1**  **super**(SuperClassName, **self**).methodName(variables)  **Option #2**  \_ClassName\_\_method\_name(variables) | **Invoking a Class Constructor:** Use the class name followed by two parenthesis. Example for class “Stack”:  **Example:** my\_stack = **Stack()**  **Class Special Methods:** **\_\_**name**\_\_** Always preceded and proceeded by two underscores.  **@property:** Class methods that do not require parenthesis when called. Typically return an object or primitive.  **Static Method: @staticmethod**  Called using the **class name** not an object name.  **Example:** ClassName.static\_method() | **Inheritance and Classes:** Python class can inherit multiple classes.  **Class and Inheritance Functions:**   * **type**(variable\_name): Returns a formatted string of object’s class name. * **isinstance**(variable\_name, ClassName): Returns True if variable is of type ClassName, False otherwise.   **Example:** *isinstance*(my\_stack, Stack) returns True.   * **issubclass**(SubclassName, ClassName): Returns true if SubclassName is a subclass of ClassName.   **Example:** *issubclass*(Stack, object) returns True. | **Abstract Classes**  Requires the import:  **from** abc **import** ABCMeta, **abstractmethod**, **abstractproperty**  # Required first line for abstract class  **\_\_meta\_class\_\_ = ABCMeta**  **@abstractmethod**  **def** my\_method(*args*):  **pass**  **@abstractproperty**  **def** my\_method(*args*):  **pass**  **Abstract classes do NOT inherit ABCMeta.** |

**Exceptions**

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| **Format for an Exception**  **try:**  **pass**  **except** ErrorTypeName **as** error\_object:  # Catches only error of type ErrorName  **pass**  **except:**  # Catches all exceptions  **pass**  **finally:**  # Always run  **pass** | **Creating Your Own Exception**  **class** **MyException**(exception):  **def** \_\_init\_\_(self, errno, msg):  self.args = (errno, msg)  self.errno = errno  self.msg = msg  **class** MyException2(exception):  **pass** | **Throwing an Exception**  Use the **raise** keyword  **raise** MyException(404, “Access Forbidden”) |

**Modules, Importing, and the sys Toolset**

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| **Importing From a Module with Normal Namespace**  **Syntax: import filename**  Filename is the python filename without the file extension (.py). When importing in this fashion, it uses the file name as the namespace for the functions/classes in that file.  **Example:** Python file div.py has a function called divide that divides to integers.  **import** div  print **div.divide**(4,2)  **Importing From a Module with a New Namespace**  **Syntax: import** filename **as namespace**  Use a custom namespace name for  **Example:** Python file div.py has a function called divide that divides to integers. New namespace is named “foo”  **import** div **as** **foo**  print **foo**.divide(4,2) | **sys – Common System Functions**  **import** sys  **Command Line Arguments:**  **sys.argv**  **Quitting Python:**  **sys.exit(0)**  **Printing to the Console (Substitute for print):**  **sys.stdout(“Hello World”)**  **Getting User Input from the Console:**  input = **sys.stdin.readline()** | **Function to Add Set of Integers**  **Passed by Command Line**  **import** sys  def sum\_command\_line\_args()  input\_args = **sys.argv**  sum = 0  **try:**  # Skip element one since module name  **for** i **in** range(**1**, *len*(input\_args)):  sum += *int*(input\_args[i])  **catch:**  *print* “Input argument not an integer”  **sys**.**exit**(0)  # Print the sum to the console.  *print* “The sum of the input arguments is: “,  *print* sum\_command\_line\_args() |

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| **Documentation String**  **Documentation String:** First statement of a module, class, or function.  **Extracting Documentation String for a Function, Class, or Module:**  Use the method **\_\_doc\_\_**  **Example:** A function exists called fact. To print its documentation string, call:  *print* fact.\_\_doc\_\_  **Accessing Documentation String Outside a Python Program**  **Example:** Function *fact* exists in module MyModule.py  **Interpretative Mode:**  **import**(MyModule)  **help**(MyModule.fact)  **Command Line:**  **pydoc** MyModule.fact | **Unit Testing**  Included in **Documentation String**.  **Module Name:** **doctest**  **Unit Test Function Name:** testmod()  **Format:**  **>>>** function\_name(*args*)  *result*  **Example:**  **def** multiply(*a, b*):  “””  >>> multiply (0, 1)  0  >>> multiply (2, 1)  2  >>> multiply (3, -1)  -3  “””  **return** a \* b  **Setting Up doctest in Supporting Modules**  # Check to see if this module is main  **if**( \_\_name\_\_ == ‘main’)**:**  # Import doctest module then run testmod()  **import** doctest  **doctest.testmod()** |

**Benefits of Python**

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| Good string and list processing functionality which minimizes awkward additional coding. | Scripted/interpreted coding available for testing |
| Higher order function support (e.g. functions can take other functions as arguments) | Syntax is comparable to other languages. |
| Good set of built-in libraries. | Wide range of free libraries and projects to build off. |
| People outside AI use it so others can appreciate your code. |  |

**Midterm Special Notes**

**Python:**

1. Do not forget colons in Python code including after function definitions, for, while, and if statements.
2. Do not forget to call imports in Python code for modules such as math, random, and sys.
3. Printing a formatted string of numbers can be written:

print “%3d %0.2f” % (10, .9799) # Prints 10 with a preceding space and 0.98

1. It is possible to have Tuples of size 0 by doing:

x = ()

1. It is possible to have Tuples of size 1 by doing:

x = “Hello World”,

x = (“Hello World”,)

1. For an abstract class, you need the line:

\_\_metaclass\_\_ = ABCMeta

**General Agents:**

1. **Components Needs to Pass the Turing Test:**
   1. **Natural Language Processing**
   2. **Knowledge Representation** (i.e. storage paradigm)
   3. **Automated Reasoning**
   4. **Machine Learning**
2. **Cognitive Science:** Brings together computer models from AI and experimental techniques from psychology to construct precise and testable **theories of the human mind.**
3. **Agent Function** – Maps percept sequence to agent action.
4. **Simple Reflex Agent** – Select actions based off the **current percept only.** Often defined by **condition-action rules** (i.e. **productions**)
5. **Goal Based Agents** – A **goal** is a binary condition (i.e. either met or not met). A goal based agent tries to reach a target goal. **Search and planning agents** may be goal based agents.
6. **Problem solving agents** deal with **atomic environments** (i.e. the environment is treated as a single whole and is **indivisible**).

**Search:**

1. In Recursive Best First Search code, remember to do the Goal\_Test at the beginning of the function and to check if the successors list is empty after creating it.
2. Effective Branch Factor: Equivalent branch factor if the search tree was modelled as a balanced tree (i.e. where the number of children for each node is equivalent for all nodes).

**Constraint Satisfaction:**

1. **Node Consistent Variable** – Any variable where every value in the variable’s domain **satisfies all of its unary constraints** in a CSP network.
2. In AC-3, only excluding the current paired variable are expanded.
3. **Local Consistency:** Given a constraint graph, enforcing consistency (i.e. ensuring variables satisfy constraints) locally **in each part of the graph** leads to invalid values being eliminated throughout the graph.
4. **Path Consistency** – **A two variable set are path consistent with respect to a third variable**  if for every assignment of values to and consistent with the constraint , there is a valid assignment to that satisfies the constraints and .
5. **Interleaving Search and Inference** AC-3 can be used to infer reductions in the search domain both **before and during search**.
6. **Forward Checking** – One way to implement “Inference” in Backtracking algorithm. Whenever a variable is assigned, establish arc consistency for it on all unassigned variables. If arc consistency checking was done in preprocessing, forward checking adds no value.
7. **Minimum Remaining Value (MRV), Fail First, Most Constrained Variable Heuristic:** Select the variable to assign next that has the smallest inferred domain (i.e. least remaining legal values).

**Logic and Logic Agents**

1. Declarative Programming: Provide information to the agent on information it needs to know and it figures out how to achieve the solution. De Procedural approach: Teach the agent how to do certain actions and it uses that information to figure out a solution to what you intend for it to do.
2. **Background Knowledge** – Initial knowledge in the knowledge base.
3. **Inference** – Deriving new sentences from existing sentences.
4. **Logical Connectives:** Used to construct complex sentences out of atomic sentences.
5. **Theorem Proving:** Using sentences already in the model, apply **rules of inference** to construct a proof of the desired sentence without consulting models.
6. **Entailment Between Sentences: When one sentence logically follows from another sentence or set of sentences. It is similar to implies in philosophy.**
7. **Logical Inference:** **Process of drawing conclusions (i.e. new sentences) through entailment**. **Symbol of Inference:** ˫ Given a knowledge base, *KB*, and a sentence *α*, if an inference algorithm, *i*, inferred *α* from *KB* then:
8. **Sound or Truth Preserving Inference Algorithm:** Can only **derive** entailed sentences. **Hence it cannot prove any sentence that is wrong.** **Example:** Model checking is a sound algorithm since it does not work on infinite spaces.
9. **Complete Inference Algorithm:** Can **derive** any entailed sentence. **A complete inference algorithm can prove anything that is right.**
10. **Literal:** In a complex sentence, a literal is either an atomic sentence (i.e. **positive literal**) or its negation (i.e. **negative literal**).
11. **Proof:** A chain of conclusions that leads to the establishing some statement following from the knowledge base.

**General:**

**Inferences, Proofs, and Resolution**

**Three Key Notions in Propositional Logic**

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| **Logical Equivalence:** | **Validity** – A statement that is true in all models. | **Satisfiability** – A statement where at least one model can make the statement true. |

**Propositional Proof** – A series of steps where each statement is either from the knowledge base, a valid propositional statement, or a statement follows previous statements via some rule of propositional inference.

**Framing a Proof as a Search Problem**

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| A propositional logic proof can be treated as search problem and existing search algorithms can be used to find a valid proof. | **Initial State:** The initial knowledge base | **Actions:** Set of all inference rules applied to all the sentences that match the first half of an inference rule | **Results:** Add the bottom half of all applicable inference rules (see actions) to the knowledge base. | **Goal:** A knowledge base that contains the statement that is trying to be proven. |

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| **Monotonicity** – Property of some knowledge bases where the set of entailed sentences only increases as sentences are added to the knowledge base. | **Nonmonotonic logics** – Common in the study of human AI. Set of entailed sentences may decrease. | **Literal** – Propositional variables or their negation. Example: or |

**Resolution**

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| **Resolution** is a **sound** and **valid** **inference rule**.  Requires **two disjunctive clauses**. If the clauses contain complimentary variables, thetwo **clauses are combined with complementary literals excluded**. | **Example of Resolution:**  **Resolvent:** Clause produced by resolution. (i.e. bottom line of inference specifically: ) | **Complementary Literals** – One literal is the negation of the other literal.  **Unit Resolution:** Right hand clause contains a single literal whose complement is in the left clause.  **Clause Set Notation:** is the same as a disjunction of those literals. |

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| **Conjunctive Normal Form (CNF):** Conjunction (ANDs) of disjunctions (ORs).  **Resolution works best on propositional knowledge bases in CNF**. | **Truth Table Approach to Convert to CNF**   * Enumerate all models. * For any model that is false, take a disjunction of the literals negation.   **Example:**   |  |  |  | | --- | --- | --- | | **A** | **B** | **Result** | | True | True | False | | True | False | True | | False | True | False | | False | False | True | | **Inference Algorithm Approach to Convert to CNF**  **Key Inference Steps:**   * **Double negation** * **DeMorgan’s Theorem** * **Biconditional Elimination** * **Distributivity** * **Implication Elimination**   **Example:** |
| **Using CNF with Resolution**  **Goal:** Prove  **Step #1:** Use implication elimination  **Step#2:** Negate the goal  **Step #3:** Convert to CNF  **Step #4:** Prove the statement is not satisfiable (i.e. the empty clause is found through resolution). |

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| **Resolution Closure:** Set of all statements that derive from the knowledge base through resolution. | **Resolution Refutation Stops in Two Cases:**   1. **Empty clause found** 2. **No new clauses are possible in the resolution closure.** | **Refutation** – Empty clause found when performing resolution. |

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| **Definite Clause** – Disjunctive (OR) clause with **exactly one positive literal**.  **Example:** | **Notation for Definite Clause:**  Example:  **ASCII Notation:** | **Head:** Positive literal in the clause (e.g. )  **Tail:** Negative literals if any (e.g. , )  **Rule:** Entire clause. |

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| **Horn clause:** Disjunctive clause with **at most one positive literal**.  **Example Horn Clause:**  **Alternative Notation:** | **Horn clause:** Collection of Horn clauses. A type of **logic program**.  **Importance of Horn Clauses and Program:** Knowledge bases that are **Horn programs** can decide if a clause is entailed in **linear time and space**. | **Goal:** See if  **Backward Chaining:** If KB is a Horn program, look for a clause where B is the head. Check for a rule where the head is true. If one is found, then continue search.  **Forward Chaining:** If KB is a Horn program, start from the facts and **search forward until no possible change to KB or the goal is found**. | |  |  | | --- | --- | |  | (Fact) | |  | (Fact) | |  | (i.e. ) | |  | (i.e. |   **Backward Chaining**  Finds then then then  **Forward Chaining**  Finds then then then |

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| **Closed World Assumption (CWA)** – Facts that are not known are assumed to be **false**. This favors **minimal models**. | **Open World Assumption (OWA)** – Facts that are not known are assumed to be **true**. This favors **maximal models**. |

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| **DPLL** – Resolution Finding Algorithm  **Three Optimizations Over the Basic Resolution Algorithm:**   1. **Early Termination**: If all clauses are satisfied (have at least one positive literal) or any clause is false, terminate the algorithm. 2. **Pure Symbol Heuristic:** A **pure symbol** is any symbol that has the same sign in all clauses. Pure symbols are set to true if they exist. 3. **Unit Clause:** A **unit clause** contains on a single literal. The variable in the unit clause is set to true to satisfy the clause. | **def DPLL\_Satisfiable**(s): **# Returns True or False**    clauses = set of clauses from CNF representation of s  symbols = list of symbols in s  **return** **DPLL**(clauses, symbols, {})  **def** **DPLL**(clauses, symbols, model)**:**  **# Check Early Termination**  **if** every clause is true in model**:**  **return True**  **elif** some clause is false in model**:**  **return** **False**  **# Check Pure Symbol Heuristic**  P, value = **FIND\_PURE\_SYMBOL**(clauses, symbol, model)  **if** P **is not None:**  **return** **DPLL**(clauses, symbols – P, model U {P=value})  **# Check Unit Clause Heuristic**  P, value = **FIND\_UNIT\_CLAUSE**(clauses, model)  **if** P **is** **not** **None:**  **return** **DPLL**(clauses, symbols – P, model U {P=value})  **# Select first symbol and check both true and false**  P = **FIRST**(symbols)  rest = **REST**(symbols)  **return** **DPLL**(clauses, rest, model U {P = **True**})  **or** **DPLL**(clauses, rest, model U {P = **False**}) |

**Prolog**

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| a. – Fact A in Prolog.  b :- a – Horn Clause . Since is true, then is also true.  c :- b – Horn Clause . Since is true, then so is  d :- a, b – Horn Clause . Since and are both true, so is | This is the same as: | Prolog supports non-Horn clauses like: and |

**Question #1 from Practice Final**

**First Order Logic**

**Logic based agents** tell the knowledge base about their **percepts**.

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| **First Order Logic** – Logic system where variable domains is greater than solely “True” and “False” | **Variables:** Range over sets.  **Usual notation:** x, y, z | **Constants:** Fixed values from a set  **Usual notation:** a, b, c | **Function:** Take variables with function symbols and return a constant  **Usual notation:** f, g, h, | **Predicate:** Takes inputs and outputs True/False  **Usual notation:** P, Q, R |

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| **Term:** A variable, a constant, or built up from these using function symbols and composition. | **Atomic Formula:** Predicate where each of the predicate slots is filled by a term.  **Example:** | **Formula:** An atomic formula or a composite of simpler formula. | **Universal Quantifier:** Symbol  - For all , is true. | **Existential Quantifier:** Symbol  - For some , is true. |

**First Order Logic Semantics**

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| **Universe** () – A set over which all variables range over. | **Constant** () – A value in the universe | **Function** () – A Cartesian product defined as: | **Predicate** (): Returns True or false and is defined as: | **Language:** Set of all constants in the universe and all function symbols. |

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| **Structure/Model** ()**:** Combination of the universe, constants, functions, and predicates. | **Bound Variable:** A variable in a first order function that is within the scope of an existential or universal quantifier. | **Unbound Variable:** A variable in a first order function that has no quantifier. | **Example:**  **Unbound Variable:**  **Bound Variable:** | **Variable/Object Assignment** (): A map from unbound variables to elements in the universe () |

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| **Logic Equations with Quantifiers:** | **Dealing with Predicates and Quantifiers:**  ( is a term) | **Example:** Addition and Multiplication on Integers  **Predicate:**  **Functions:** ,  **Model:** Includes set of natural numbers | **Not in Model:**  **In Model:**  is |

**Interacting with a First Order Knowledge Base**

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| **TELL**(KB, King(John)) – Tells the knowledge base the fact that John is a king.  **TELL**(KB, Person(Richard)) – Tells the knowledge base that Richard is a person. | **Ask**(KB, King(John)) – Predicate that asks the knowledge base if John is a King. Would return true.  **Ask**(KB, King(Zayd)) – Returns false since Zayd is not a king.  This command is referred to as **query** or **goal**. | **AskVars**(KB, Person(x)) – Asks questions that returns a constant.  Query response is known as a **binding list** or **substitution**. Example return is {x/Richard} | **Example First Order Knowledge Bases**  1. Any relational database  2. Basic set theory   * No function symbols * = operator checks for equality * Constant is the empty set |

**Theorem Proving in First Order Logic**

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| **Procedure**  1. Convert all formulas in into **prenex normal form**. Prenex normal form is:  2. **Skolemize the equation** to remove any existential quantifiers.  3. If all variables are bound and only universal quantifiers, **the quantifers can be dropped and all variables are free**.  4. **Convert the open formula to CNF and use resolution to prove refutation** | **Skolemization Examples**  skolemizes to  skolemizes to | **Additional Notes**  If there are only existential quantifiers, the variables are turned into constants and existential quantifiers dropped.  To perform refutation, a substitution list may be required to ensure the terms in the predicate match. This can be checked using the **unification algorithm**. |

Model checking is possible to prove entailment in first order knowledge bases. However, the time complexity is just as bad or worse than it is for propositional logic.

\* = operator for checking two values are the same

First Order Logic Database Commands

PDDL – Planning Domain Definition Language

Successor of Strips language.

Planning – Application of first order logic. Develop a sequence of actions to achieve a goal while at each step in time satisfying all constraints.

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| **Necessary Functions for Unify Function**   * **is\_var**(z) – Checks if z is a variable. * **is\_term**(z) – Checks if parameter z is a term. * **args**(z) – Extracts a list of arguments in z   + args((z\*z)+35) – Returns (z\*z, 35) * **op**(z) – Gets the **outermost function symbol** in z   + op((z\*z)+35) – Returns “+” * **is\_list**(z) – Checks if parameter z is a list. * **head**(z) – Returns first element in list z * **tail**(z) – Returns all elements after the first element in z.   **Necessary Functions for Unify\_Var Function**   * **occur\_ck**(var, z) – Checks if z is function containing var   + occur\_ck(z, (z\*z)+35) – Returns **True**   + occur\_ck(y, (z\*z)+35) – Returns **False** * **append**(new\_sub, sub\_list) – Appends the new substitution new\_sub to the sub\_list. | **Unify**(x, y, S):  # x – a variable, constant, term, or list  # y – a variable, constant, term, or list  # S – substitution so far  # returns a Substitution list or “None”  # Check for previous failure  **if**(S == **None**)**:**  **return** **False**  # If with substitution the two parameters are the same  # then return the substitution.  **if**( x(S) == y(S))**:**  **return** S  # If x or y are variables, try to create a new substitution  **if**(**is\_var**(x))**:**  **return** **Unify\_Var**(x, y, S)  **elif**(**is\_var**(y))**:**  **return** **Unify\_Var**(y, x, S)  **elif**( **is\_term**(x) **and** **is\_term**(y) )**:**  **return** **Unify**(**args**(x), **args**(y), **Unify**(**op**(x), **op**(y), S) )  **elif**( **is\_list**(x) **and** **is\_list**(y) )**:**  **return** **Unify**( **tail**(x), **tail**(y), **Unify**( **head**(x), **head**(y), S) )  **else**:  **return** **None** | **Unify\_Var**(var, y, S):  # var – A variable  # y – a variable, constant, term, or list  # S – substitution so far  # returns a Substitution list or “None”  # Check if substitution exists for var (i.e. sub\_val1)  **if**( var |-> sub\_val1 )**:**  **return** **Unify**( sub\_val1, y, S)  # Check if substitution exists for y (i.e. sub\_val2)  **elif**( y |-> sub\_val2 ):  **return** **Unify**( var, sub\_val2, S)  # Check if y is a function f(var)  **elif**( **occur\_ck**(var, y) )**:**  **return** **None**  **else:**  **return** **append**( var |-> y, S) |

**Unification Examples – These Can Be Simplified and To Just Unify Whatever Is After the “=” Signs.**

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| **Problem:** Unify “x = f(z)” and “y = g(w)”  **Step #1:** Unify( x=f(z), y=g(w), {} )  **Step #2:** Unify( (x, f(z)), (y, g(w)), Unify( =, =, {} ) )  **Step #3:** Unify( (x, f(z)), (y, g(w)), {} )  **Step #4:** Unify( (f(z)), (g(w)), Unify(x, y, {}) )  **Step #5:** Unify( (f(z)), (g(w)), Unify\_Var(x, y, {}) )  **Step #6:** Unify( (f(z)), (g(w)), {x |-> y} )  **Step #7:** Unify( (), (), Unify(f(z), g(w), {x |-> y} ) )  **Step #8:** Unify( (), (), Unify(z, w, Unify(f, g, {x |-> y}) ) )  **Step #9:** Unify( (), (), Unify(z, w, Unify\_Var(f, g, {x |-> y}) ) )  **Step #10:** Unify( (), (), Unify(z, w, {x |-> y, f |-> g } ) )  **Step #11:** Unify( (), (), Unify\_Var(z, w, {x |-> y, f |-> g } ) )  **Step #12:** Unify( (), (),{x |-> y, f |-> g, z |-> w } ) )  **Step #13:** Returns the substitution list {x |-> y, f |-> g, z |-> w } | **Problem:** Unify “x=[g(v), f(g(z))]” and “y=[g(f(w)), f(w)]”  **Step #1:** Unify( x=[g(v), f(g(z))], y=[g(f(w)), f(w)], {} )  **Step #2:** Unify( (x,[g(v), f(g(z))]), (y, [g(f(w)), f(w)]), Unify(=, =, {}) )  **Step #3:** Unify( (x,[g(v), f(g(z))]), (y, [g(f(w)), f(w)]), {} )  **Step #4:** Unify( ([g(v), f(g(z))]), ([g(f(w)), f(w)]), Unify(x, y, {}) )  **Step #5:** Unify( ([g(v), f(g(z))]), ([g(f(w)), f(w)]), Unify\_Var(x, y, {}) )  **Step #6:** Unify( ([g(v), f(g(z))]), ([g(f(w)), f(w)]), {x |-> y} )  **Step #7:** Unify( (), (), Unify( [g(v), f(g(z))], [g(f(w)), f(w)], {x |-> y} ) )  **Step #8:** Unify( (), (), Unify( [f(g(z))], [f(w)], Unify(g(v), g(f(w)), {x |-> y} ) ) )  **Step #9:** Unify( (), (), Unify( [f(g(z))], [f(w)], Unify(v, f(w), Unify(g, g, {x |-> y} ) ) ) )  **Step #10:** Unify( (), (), Unify( [f(g(z))], [f(w)], Unify(v, f(w), {x |-> y} ) ) )  **Step #11:** Unify( (), (), Unify( [f(g(z))], [f(w)], Unify\_Var(v, f(w), {x |-> y} ) ) )  **Step #12:** Unify( (), (), Unify( [f(g(z))], [f(w)], {x |-> y, v |-> f(w)} ) ) (Exclude outer unify)  **Step #13:** Unify( [], [], Unify(f(g(z)), f(w), {x |-> y, v |-> f(w)} ))  **Step #14:** Unify( [], [], Unify(g(z), w, Unify( f, f, {x |-> y, v |-> f(w)} )))  **Step #15:** Unify( [], [], Unify(g(z), w, {x |-> y, v |-> f(w)} ))  **Step #16:** Unify( [], [], Unify\_Var(w, g(z), {x |-> y, v |-> f(w)} ))  **Step #17:** Unify( [], [],{x |-> y, v |-> f(w), w|->g(z)} ))  **Step #18:** Functions return the substitution list: {x |-> y, v |-> f(w), w|->g(z)} |

**Planning**

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| **Problem Solving Agent** – Goal based agent that is focused on solving problems on atomic domains. | **Planning Agents** – Goal based agents that work on factored domains. |

**PDDL – Planning Domain Definition Language**

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| Heavily influenced by earlier planning languages including **STRIPS** and **ADL**. | **Fluent** – Facts that may change from situation to situation. | **Ground Fluent** – Fluent contain **no variable** (i.e. only constants). They are **functionless atoms**. | **State** – Conjunction of fluents that are ground.  **States cannot contain negative atoms.** |
| **Closed World Assumption** – Fluents not in the knowledge base are false. (Used in PDDL) | **Unique Names Assumption** – Any objects that have different names are assumed to be different. | **Illegal Fluents in a State Description**   1. **Fluents containing variables**. Example: 2. **Fluents containing negations.** Example: | Fluents are a **conjunction** so fluent **order does not matter**. |

**Actions in Planning**

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| **Actions** need to clearly define what aspect of the state changes and what stays the same. | **Frame Problem:** In classical planning, most aspects of the state remain the same after an action. It can be **prohibitive to detail the countless aspect of a state that stayed the same after an action** | **Solution to the Frame Problem in PDDL:** **PDDL only enumerates the aspects of the state that change as a result of an action.** Any unmentioned aspects are assumed not to change. |

**PDDL Action Schema**

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| **Three Components in PDDL Action Schema**   1. **Action Name and Input Variables** 2. **Precondition(s) if any** 3. **Effect(s)** | **Action Name and Input Variables**  **Name** of the action performed and **any input variables**.  **Example:**  **Action Name:**  **Variables:** , , | **Preconditions**  Aspects of the state that must be true before an action can be performed. **Cannot contain negated atoms.**  **Example:** | **Effects**  Action results. Changes in state.  **Example:** | **Complete Example** |

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| **Applicable Action** – An action is applicable in state if all of action ’s preconditions are satisfied in state . | In any given state, **multiple instances of a given action could be applicable**. Example: plane could fly from to or from to | If an action has variables and the variable have a maximum domain of size , then it takes to find all applicable ground actions worst case. |

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| **Result of an Action** – Conjunction of fluents. | **Delete List** – **Negative** literals in the result of an action. These negative literals correspond to fluents **deleted from the state**. | **Add List** – **Positive** literals in the result of an action. These positive literals correspond to fluents **added to the state**. | **Note: Actions do not refer to time**. Precondition refers to time and results refer to time . |

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| **Planning Domain** – Set of action schemas. | **Initial State** – **Conjunction of ground atoms.** Hence, every slot in the fluent must be filled. | **Goal** – Conjunction of Literals. **Goals can have variables**, which are treated as existentially quantified.  **Goal Example:**  In this case, could be any plane. | **Solution** – Sequence of actions from the initial state to a **state that ENTAILS the goal**. | **Inequality Condition** – Used to prevent illegal conditions in actions where two input variables have the same value. |

**Example Planning Algorithms**

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| **PlanSat** – Given a planning problem, it determines whether a plan **exists** that solves the problem. | **BoundedPlanSat** – Given a planning problem, it determines whether a plan **exists** that solves the problem in **k steps or less**. | Both algorithms are **PSPACE** but **NP-Hard** (hard as any other problem in NP).  For problems **without negative preconditions, PlanSet is polynomial time (P)**. |

**Planning as a Search Problem**

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| **Forward State Space Search** – Start from the initial condition and search towards the solution. | **Backward (Regression) Relevant States Search** – Start from the goal and try to search backwards until a state IMPLIED by the start state is found.  Referred to as **relevant-states search** since only states relevant to the goal are explored. At each step, there may be a **set of relevant states** (not just a single state). |
| **Negatives of Forward State Space Search**  **Prone to search irrelevant states.** **Example:** Planning problem trying to go from and . Would involve searching many irrelevant states.  **Requires domain-independent heuristics since planning problems can have large state spaces.** | **Negatives of Forward State Space Search**  **Partially uninstantiated actions and states** – Since a goal will not always detail a complete state, negative relevant states search often involves handling only partially instantiated actions and states. **It must also handle ground states.** |

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| **Heuristics in Planning** – When trying to come up with a plan through search, heuristics may be helpful.  **Example Heuristic Type** – Come up with plans to relaxed problems. | **Planning Problem and Search**  **Nodes** – States in the state space.  **Edges** – Actions in the planning domain (i.e. set of schemas) | **Solution** – Path (i.e. sequence of actions) to go from the initial state **to a state entailed by the goal state**. |

**Heuristics for Search**

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| **Ignore Preconditions Heuristic**  Drop all preconditions from actions. By itself, this is NOT an admissible heuristic as it may over estimate the solution.  **Modified Approach** – Delete all effects expect those literals that are in the goal. **Then count the number of actions needed to reach the goal.**    When combined with the cost to get to the current node, **this heuristic allows you to use A\* search** to find a plan.  **Exact Count:** **NP-Hard since it does not reduce the number of states to search.**  In **P time**, can a**pproximate the cost** within factor where  **is the number of literals in the goal** | **Ignore Delete Lists**  Remove all delete lists (i.e. set of negated literals) from all actions.  Literals in the state are monotonically increase and if the goal is possible, it is eventually found.  Still leaves a problem that is **NP Hard** **since it does not reduce the number of states to search.** | **State Abstraction**  A many-to-one mapping from states in the ground representation of the problem to the abstract representation.  **Example:** In the plane cargo problem, require that all packages have the same destination (e.g. a hub) and that packages can only start in one of five airports.  **This usually entails ignoring some fluents.** |

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| **Decomposition** – Key ideal in defining heuristics. It entails dividing a problem into parts, solving each part individually and then combining the parts. Similar to divide and conquer algorithm. | **Subgoal Independence Assumption** – Cost of solving a conjunction of subgoals is approximated by the sum of the costs to solve each subgoal independently.  **This assumption can be optimistic or pessimistic**. Optimistic if when solving each subgoal, actions that would otherwise cancel each other do not. Pessimistic as there **may be redundant actions**. |

**Planning Graph**

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| **Planning Graph** – Special data structure used to give better heuristic estimates for the cost of a plan.  **Polynomial size approximation** of the tree one would get by exploring all actions.  Useable for **propositional planning problems only**. | Level – Organizational structure for a planning graph.  Each level is denoted as   * – **Initial State**   Each level is linked by a set of possible actions.   * – Set of all possible actions possible in level | In each level, the set of achieveable literals are shown. **For a given , both the positive () and negative () could hold** given different sets of actions.  and alternate in the tree.  Action :   * Preconditions: * Effects: |

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| **Persistence Action** – Type of no-op. Used to preserve/persist any literal which is not negated by an action.  Every literal has a persistence action (small square in action) from to in the planning graph.  **Once a literal appears in a level it remains present for all future levels of the planning graph**. | **Mutex** – Mutual exclusion. Curved links to indicate things (e.g. actions, literals, etc.) that cannot occur at the same time. | **Leveled Off** – When two consecutive levels of a graph are identical.  This is the **termination condition of the planning graph**. | Given graph with literals and actions:   * – Nodes maximum in each * – Mutex links in each * – Maximum number of nodes in each * – Mutex links in each * – Effect and precondition links because each persistence action goes to one effect and one precondition link and every standard action could go to precondition and effect links.   Hence, for an level planning graph, the maximum size is **which is polynomial space. The construction time is equivalent.** |

**Using Planning Graphs for Heuristic Estimation**

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| **Unsolvable Planning Problem:** Goal does not appear in the final step in the planning graph. | **Level Cost of**  - First level in the planning graph where goal literal first appears. | **Three Methods to Estimate Conjunction of Goals**   1. **Max-Level** 2. **Level-Sum** 3. **Set Level** | **Max Level** – Largest level cost amongst all the goal literals.  **Admissible.** | **Level Sum** – Sum of the level costs of all goal literals.  **Inadmissible** | **Set-Level** – Level in the graph **where all literals in the SET of goal literals first appear**.  **Admissible.** |

**Practice Final Question #4**

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| **Variables** | **Predicates**   * – Checks if is a foot. * – Checks if is a sock. * – Checks if is a shoe. * - Checks if is bare. * – Checks if has on a * - Checks if is off * - Checks if has a shoe on. * – Checks if is off. * – Checks if and are from same side (left/right) |  | **Example Plan** |

**Decision Theory and Decision Theory Agents**

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| Previous agents dealt with the world assuming everything was either: true, false, or unknown. | **Rational Decision** – Dependent on the relative importance of various goals and the likelihood (and degree/extent to which) these goals can be achieved. | **Example:**  Not always true since you can have a toothache for reasons other than a cavity. | **Possible Solution:**  This solution can be prohibitive since not all causes may be known or there are too many to enumerate individually. |

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| **Decision Theory** – Takes the utility of all possible agents and adds it to some calculation based on the probability of achieving each of the possible goals. | **def** DT\_Agent(percept)**:**  # Returns an action  **persistent** belief\_state # Probability belies about the current state of the world  **persistent** actions # Set of agent actions.  # Update set of probabilities based on percept and set of available actions  **update belief\_state** based on action and percept  **for** action\_i **in** actions:  **calculate outcome\_probability\_i** based off action description and belief state  **select action with highest expected utility** given outcome\_probability and utility information  **return** action |
| **Preference** – The extent to which the agents prefers certain goal states/**outcomes** to others.  **Example:** An agent may prefer coffee twice as much as tea. |
| **Utility Theory** – Used to represent and reason about preferences. Utility theory says that every state has a degree of usefulness (i.e. utility) to an agent and that the agent prefers states with high utility. |
| **Maximum Expected Utility (MEU)** – Agent should choose the action which yields the highest expected payoff among the available choices. |

**Probability**

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| **Sample Space (Ω)** – Set of all possible worlds. In other words, they are the set of all things that could be world.  Elements in the sample space are **mutually exclusive**.  **Example:** Sample space for rolling two six sided dice is: (1,1), (1,2), … (2,1), …(6,6) | **Probability Model/Probability Distribution** – Associate a number, , between 0 and 1 with each element (ω) in the sample space (Ω) with the condition that: | Probabilistic assertions may not be about individual worlds. Rather, it may deal with sets of them.  Example: Probability of the sum of a two dice roll equaling 11 entails the case of (6,5) and (5,6).  **Events** – Set of all possible worlds where a corresponding proposition holds (e.g. rolling 11). |

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| **Unconditional or Prior Probability** – Degree of belief that a proposition holds in the absence of any other probability.  **Example:** or for two dice roll. | **Evidence** – Additional information that may reveal information about the probability of other events. | **Conditional Probability** – Probability factoring in evidence from events. It is defined as:  **for > 0**  **Example:**  is: | **Notation for Probability Theory**   * **Variables** – Initial capital letter * **Value from Domain/Sample Space** – Initial lower case letter |

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| **Random Variable ()** – A function that maps elements (ω) from the sample space (Ω) to the set of real numbers.  **Example Random Variable:** Bet $3 on whether a coin flip is heads or tails. The random variable could be: | **Domain Variable** – Enumerate possible elements in the state space. There are **DIFFERENT from random variables** as they may not map to the set of real numbers.  **Example Domain Variable:** | **Joint Probability Distribution** – Probability distribution of the Cartesian product of two or more random variables.  **Example:**  Joint probability distributions **allow us to discuss probability for sentences involving AND ()**:  **Example:** |

**Random Variable Classifications**

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| **Boolean Random Variable** (also known as an **Indicator Random Variable**) – Random variable where **each point in the sample space is mapped to one of two values**. | **Discrete Random Variable** – Random variable where the sample space is finite or if the image of the random variable is a subset of the integers. | **Continuous Random Variable** – Usually has a domain that consists an infinite number of states and where the function is continuous on the domain.  **Example:** Sample space could be points in a room and random variable could be the temperature at a point in degrees Celsius.  Calculating **probabilities of continuous random variables usually involves computing an integral**. |

**Important Probability Functions**

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**Random variables** often have interrelated values. Example: Probability of a toothache, cavity, and dentist catching your gums are related.

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| |  |  |  |  |  | | --- | --- | --- | --- | --- | |  | Toothache | | ¬Toothache | | |  | Catch | ¬Catch | Catch | ¬Catch | | Cavity | 0.108 | 0.012 | 0.072 | 0.008 | | ¬Cavity | 0.016 | 0.064 | 0.144 | 0.576 |   Joint Probability Distribution for Random Variables , , and .  This approach is not scalable with large numbers of random variables as it **grows a rate of for random variables**. | **Marginal Probability** – Probability of a single random variable or single random variable’s state without dependence on other random variables. | **Marginalization/Summing Out** – Given a joint probability function, of two random variables, and , the marginal probability of random variable is found by:  **Example:**  **Note the resulting probability is a VECTOR.** | **Conditioning** – Dependent on the conditional probabilities to find the marginal probability of through:  **Note the resulting probability is a VECTOR.** |

**Conditioning Example**

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| **Example:** Find the conditional probabilities and . | Both and contain . Hence this can be simplified to: | Hence, is: | **Normalization Constant (α)** – Used to simplify calculations and to ensure the results each the expected value (e.g. 1 for probabilities) |

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| **Independence** – Random variable states do not affect one another. **Hence, joint probability distributions can be factored into separate disjoint distributions.**  When and are independent: | **Bayes’ Rule**  Given two non-independent random variables and , then:  Hence: | **Importance of Baye’s Rule:** If you need to know , it is hard to find but you know, , you can use Baye’s rule in combination with marginal probabilities to solve for  **Example:** 70% of people with meningitis have a stiff neck. Odds of meningitis are 1/50000 (0.00002) and the odds of a stiff neck are 1/100 (0.01). The probability of is: |

**Learning**

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| **Learning** – Process by which an **agent improves its performance on future tasks after making observations about the world**. | **Applications of Learning**   1. **Programmer could not predict all possible situations an agent could encounter.** 2. **Programmer cannot predict changes over time.** 3. **Programmer might not have any idea to program a solution to the same problem themselves.** | **Component Improvements and Available Learning Techniques Depend On**   1. **Component to be improved.** 2. **Prior knowledge the agent has.** 3. **The representation used for the data and the component.** 4. **Available feedback to learn from.** |

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| **Inductive Learning** – Learning from a set of input/output pairs and generating a general function that governs those pairs.  Input is usually a **vector of attribute values.** | **Deductive/Analytic Learning** – Start from a set of general rules and **derive things logically entailed from these general reules**. | **Unsupervised Learning** – Agent learns patterns from the input although no explicit feedback is supplied.  **Example:** **Clustering** – Input examples are **grouped into potentially useful clusters**. | **Reinforcement Learning** – **Agent learns through a series of reinforcements** (rewards or punishments).  **Example #1:** Lack of a tip at the end of a journey gives the taxi agent it did something wrong.  **Example #2:** Winning for a chess playing agent is a reinforcement it did something right. |

**Supervised Learning**

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| **Supervised Learning** – Agent observes input-output pairs and **learns a function that maps from the input to the output**. | **Semi-supervised Learning** – Given a few labeled examples, the agent must make what it can from a large set of unlabelled examples. | **Training Set** – Set of original input-output pairs, which are defined as:  These are generated by some unknown function, , defined as: | **Hypothesis** – A learned function **that approximates the unknown function** |

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| **Test Set** – Disjoint from the training set. **Used to test the quality of the hypothesis** function | **Classification** – Learning problem where the output  **is a finite collection of values**. | **Regression** – When the **output is always a number (often an infinite range)** | **Consistent Hypothesis** – Any hypothesis function that agrees (i.e. is consistent) with all input-output pairs.  A given set of data **may have multiple consistent hypotheses**. | **Ockham’s Razor** – Always prefer the **simplest hypothesis**.  **Definition of “Simplest” may vary.**  **Example of a Simpler Hypothesis** – First order polynomial versus degree 7 polynomial. |

**Decision Trees**

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| **A supervised learning algorithm**  Takes a vector of input attributes and returns a **single output value**.  Input attributes can be either continuous or discrete.  Focus of this class is on Boolean decision trees. Hence the outputs are either:   * **Positive Examples** return **true** * **Negative Examples** return **false**   **Leaf nodes** correspond to the **decision tree’s result**. **Internal nodes** corresponding to **one of the input attributes**.  Not all paths (branches) in a decision tree need to be the same length. | **Initial Call:** decision\_tree = **Decision\_Tree\_Algorithm**(all\_examples, all\_attributes, {})  # Builds a decision tree  **def** **Decision\_Tree\_Algorithm**(examples, attributes, parent\_examples):  # examples – Remaining unclassified examples  # attributes – Remaining attributes not yet in the tree  # parent\_examples - Set of all examples in this node’s parent.  # No examples match this classification so return most common value for set of parents  **if**( **len**(examples) == 0 )**:**  **return** **PLURALITY\_VALUE**(parent\_examples)  # All examples agree so return the agreed upon classification  **elif**( all examples have same classification )**:**  **return** classification  # Since no attributes remaining, take most common value from remaining examples  **elif**( **len**(attributes) == 0): **return** **PLURALITY\_VALUE**(examples)  **else:**  # Find the most important attribute  A = argmax\_(a in attributes)**Importance**(a, examples)  # Create a new tree  tree = **DecisionTree**()  # Iterate through all attribute values.  **for** v\_k **in** A**:**  subset\_examples = { exs **in** examples **and** E.A == v\_k }  subtree = **Decision\_Tree\_Algorithm**( subset\_examples, attributes – A, parent\_examples)  # Add the subtree to the tree  tree.**add\_branch**( v\_k, subtree )  **return** tree |
| **Important Pseudocode Functions and Methods** |
| **Plurality\_Value**(examples) – Returns the most common boolean result from the set of examples |
| **Importance**(attribute, examples) – Returns a value quantifying the importance of attribute for the set of examples. |
| **DecisionTree**() – Python style constructor for an object of class DecisionTree |
| **add\_branch**(attribute\_value, subtree) – Method to append a subtree to the tree with the edge having the value “attribute\_value”. |

**Decision Tree Importance Function**

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| **Importance** function in the decision tree algorithm selects the next attribute in the tree. | **Good attribute selections** result in example sets that contain **either only positive or only negative examples**. | **Bad attribute selections** result in example sets that have the same proportion of positive and negative examples. | **Information Gain** – Quantifies the quality of an attribute selection. |

**Entropy**

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| **Entropy** – Fundamental quantity in information theory. It is a measure of the uncertainty of a domain variable.  **The higher the entropy, the higher the uncertainty.** | **Entropy of a Boolean Random Variable :**  **Entropy of an Attribute in a Decision Tree:**  where is the number of positive examples and is the number of negative examples. | **Information gain** is defined as:  For an attribute, , in a decision tree, this simplifies to:  is a weight sum of the entropy of each random variable and its likelihood of occurring: |

**Neural Networks**

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| **Neurons** – Type of brain cell. Electrochemical activity in the network of neurons is responsible for most mental activity. | **Benefits of Neural Networks**   1. **Perform distributed computation.** 2. **Tolerate noisy inputs** 3. **Learn** | Neural networks are composed of nodes or **units** called neurons. | **Basic Neuron Structure**  Each input link has a different weight as shown as the **thickness of the input arrow**. |

**Neuron Structure**

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| A neuron is a link from unit to unit j that propagates the **activation signal** from to .  **Note the activation signal is different than the activation function.** | **Weight ()** – Numeric value which determines the **strength and sign of the connection**. | Output of the Unit is derived from the **weighted sum function ()** which is defined for **unit j** as: | **Activation Function ()** – From the weight function, it derives the neuron ’s output (). It is defined as:  Each neuron has a **single output that can be fed into several other neurons**. |

**Types of Activation Functions ()**

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| **Threshold Activation Function** – Output is binary (i.e. 0 or 1) depending on the weighted sum function’s () value and the threshold value. | **Logistic Function** – A sigmoid curve in an “S” to mark the transition as more gradual.  Logistic-curve.svg.png  **Common Function for Logistic Function:** | **Perceptron** – Uses a **threshold activation function** in the neural network’s neurons.  **Sigmoid Perceptron** – Uses the **logistic function** in the neural network’s neurons. |

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| **Feed-forward network** – Neuron connections are only in a single direction. Hence, back connections are not permitted. | **Recurrent Networks** – Outputs of neurons are allowed to go back and serve eventually as its own input.  Can lead to oscillation in result but are more realistic. | Feed-forward networks are usually arranged into **layers** where **each layer only receives inputs from the previous layer**. | **Hidden Layer** – Any layer that is not connected to either an input or an output. |

**Practice Final Questions**

1. **Mod3(x\_1, ..., x\_n) is the propositional formula which returns true if the number of variables `x\_i` which are true in a truth assignment is exactly 0 mod 3. Write down a CNF formula for Mod3 in the case where `n=6`.**

This uses the truth table\Karnaugh map approach to solve the problem. In the truth table, any assignment that makes the result false is added to the CNF as single clause that is the disjunction of the literals in the assignment but negated.

1. **Give the DPLL algorithm and explain each of the three main "shortcuts" it checks for.**

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| **DPLL** – Resolution Finding Algorithm  **Three Optimizations Over the Basic Resolution Algorithm:**   1. **Early Termination**: If all clauses are satisfied (have at least one positive literal) or any clause is false, terminate the algorithm. 2. **Pure Symbol Heuristic:** A **pure symbol** is any symbol that has the same sign in all clauses. Pure symbols are set to true if they exist. 3. **Unit Clause:** A **unit clause** contains on a single literal. The variable in the unit clause is set to true to satisfy the clause. | **def DPLL\_Satisfiable**(s): **# Returns True or False**    clauses = set of clauses from CNF representation of s  symbols = list of symbols in s  **return** **DPLL**(clauses, symbols, {})  **def** **DPLL**(clauses, symbols, model)**:**  **# Check Early Termination**  **if** every clause is true in model**:**  **return True**  **elif** some clause is false in model**:**  **return** **False**  **# Check Pure Symbol Heuristic**  P, value = **FIND\_PURE\_SYMBOL**(clauses, symbol, model)  **if** P **is not None:**  **return** **DPLL**(clauses, symbols – P, model U {P=value})  **# Check Unit Clause Heuristic**  P, value = **FIND\_UNIT\_CLAUSE**(clauses, model)  **if** P **is** **not** **None:**  **return** **DPLL**(clauses, symbols – P, model U {P=value})  **# Select first symbol and check both true and false**  P = **FIRST**(symbols)  rest = **REST**(symbols)  **return** **DPLL**(clauses, rest, model U {P = **True**})  **or** **DPLL**(clauses, rest, model U {P = **False**}) |

1. **(a) Let `x:= f(z)` and `y:= g(w)` explain how the unification algorithm from class would work on these inputs. (b) Now suppose `x:= [g(v), f(g(z))]` and `y:= [g(f(w)), f(w)]`. Explain how the unification algorithm from class would work on these inputs**

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| **Step #1:** Unify(“f(z)”, “g(w)”, {})  **Step #2:** Unify(“z”, “w” , Unify(“f”, “g”, {}) ) **# Remove operator**  **Step #3:** Unify(“z”, “w” , Unify\_Var(“f”, “g”, {}) ) **# Operators become variables**  **Step #4:** Unify(“z”, “w” , { f |-> g } ) **# Return of Unify\_Var**  **Step #5:** Unify\_Var(“z”, “w” , { f |-> g } ) **# Unify the variables**  **Step #6:** { f |-> g, z |-> w } **# Final Substitution** | **Step #1:** Unify(“[g(v), f(g(z))]”, “[g(f(w)), f(w)]”, {}) **# Remove the head of the lists.**  **Step #2:** Unify(“[f(g(z))]”, “[f(w)]”, Unify( “g(v)”, “g(f(w))”, {} )) **# Remove outermost function symbols g.**  **Step #3:** Unify(“[f(g(z))]”, “[f(w)]”, Unify( “v”, “f(w)”, Unify(“g”, “g”, {} )) **# No unification required since function operators are identical**  **Step #4:** Unify(“[f(g(z))]”, “[f(w)]”, Unify( “v”, “f(w)”, {} ) **# Unify on variable v**  **Step #5:** Unify(“[f(g(z))]”, “[f(w)]”, Unify\_Var( “v”, “f(w)”, {} ) **# Append to substitution list for variable v**  **Step #6:** Unify(“[f(g(z))]”, “[f(w)]”, { v |-> f(w) } ) **# Extract the first item in each list.**  **Step #7:** Unify(“[]”, “[]”, Unify( “f(g(z))”, “f(w)”, { v |-> f(w) } ) ) **# Extract function symbol f on the two functions**  **Step #8:** Unify(“[]”, “[]”, Unify( “g(z)”, “w”, Unify( “f”, “f”, { v |-> f(w) } ) ) ) **# Unify on identical function symbols f**  **Step #9:** Unify(“[]”, “[]”, Unify( “g(z)”, “w”, { v |-> f(w) } ) ) **# Perform Unify var on variable w**  **Step #10:** Unify(“[]”, “[]”, Unify\_Var( “w”, “g(z)”, { v |-> f(w) } ) ) **# Append substitution list for variable w**  **Step #11:** Unify(“[]”, “[]”, “w”, “g(z)”, { v |-> f(w), w|-> g(z) } ) **# Identical unification lists so no step here**  **Step #12:** { v |-> f(w), w|-> g(z) } **# Final Substitution** |

1. **Consider the problem where you have two socks and two shoes all of which are on the ground. You also have two feet. Your goal is to put on your shoes. Your feet can wear socks, but not shoes directly. Your available actions are to put on socks and put on shoes. Formulate this problem reasonably in PDDL. Then give an example plan solving it.**
2. Show how the Graphplan algorithm would work on the example of the previous problem.
3. Define the following terms related to knowledge engineering: (a) ontology, (b) reification, (c) taxonomy.
4. **Explain and give an example of the following concepts from probability theory: (a) random variable, (b) marginalization, (c) Bayes’ rule.**

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| A **random variable** () maps elements in the state space (Ω, i.e. the set of possible, disjoint worlds), to the set of real numbers. Hence:  **Example**: We bet $3 on the result of a coin flip. A random variable could be: | **Marginalization** is the extraction of probability of a single random variable from a joint probability distribution function.  **Note these are vectors.**  Example:   |  |  |  | | --- | --- | --- | |  | Toothache | ¬Toothache | | Cavity | 0.1 | 0.2 | | ¬Cavity | 0.3 | 0.4 | | **Bayes’ Rule** comes from conditional probability which is defined as P(A) given B or:  Using , it can be shown:  Example: Probability of a stiff neck if you have meningitus is 0.7. Probability of meningitus is and the probability of a stiff neck is 0.01. Hence the probability you have meningitus given a stiff neck is: |

1. **Consider the following training set of 4-tuples.**

**(T,T,T, F)**

**(T,T,F, F)**

**(T,F,T, F)**

**(T,F,F, F)**

**(F,T,T, T)**

**Here `T` is short for true, `F` is short for false. The first three columns correspond to the variables `x\_1`, `x\_2`, `x\_3`, the last column is the output of some function `f`. Calculate `Gain(x\_i)` for `i=1,2,3`. Which variable should we use as the top of a decision tree for `f`?**

To calculate the information gain for each parameter, you only need to calculate the of each attribute . The attribute with the lowest is the one to selected. Hence:

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Since has the lowest remainder, it is the attribute that should be expanded at the top of the tree. This also makes intuitive sense as results in sets containing only positive or only negative examples.

1. **Give the formal definition of perception. Explain and give an example of a feed forward network is and what a recurrent network is.**
2. **Give and explain the update rule for learning neuron weight from class.**